



Universitat
de les Illes Balears



TRAM:

*The New Numerical Model of Meteo-UIB
Suited for All Kinds of
Regional Atmospheric Predictions*

Romu Romero

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RESEARCH ARTICLE

TRAM: A new non-hydrostatic fully compressible numerical model suited for all kinds of regional atmospheric predictions

R. Romero 

Grup de Meteorologia, Departament de Física, Universitat de les Illes Balears, Palma de Mallorca, Spain

Correspondence

R. Romero, Grup de Meteorologia, Departament de Física, Universitat de les Illes Balears, Ctra. de Valldemossa km. 7.5, Palma de Mallorca 07122, Spain.
Email: romu.romero@uib.es

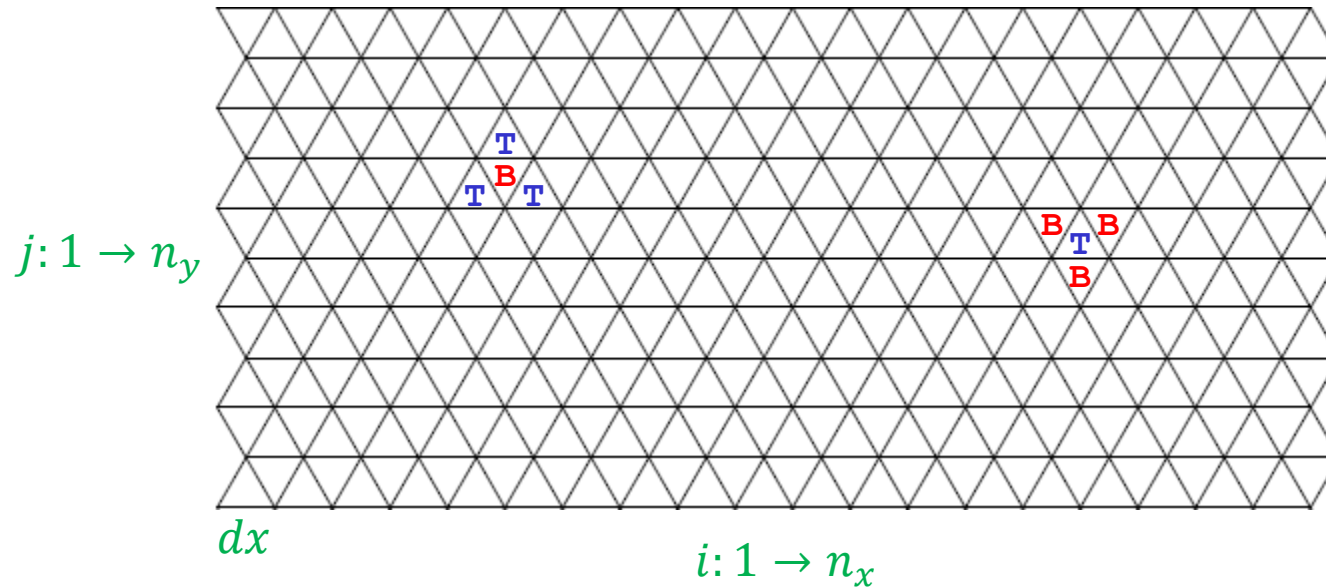
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Abstract

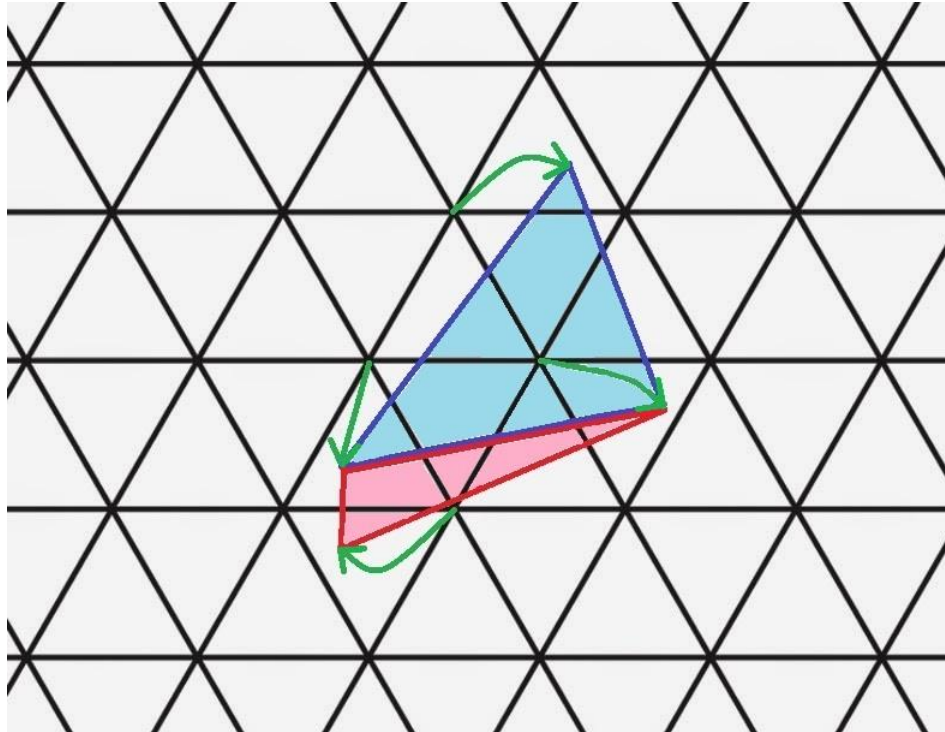
A new limited-area numerical model (TRAM, for Triangle-based Regional Atmospheric Model) has been built using a non-hydrostatic and fully compressible version of the Navier–Stokes equations. Advection terms are solved using a Reconstruct–Evolve–Average (REA) strategy over the computational cells. These cells consist of equilateral triangles in the horizontal. The classical z -coordinate is used in the vertical, allowing arbitrary stretching (e.g., higher resolution in the Planetary Boundary Layer, PBL). Proper treatment of terrain slopes in the bottom boundary conditions allows for accurately representing the orographic forcing. To gain computational efficiency, time splitting is used to integrate fast and slow terms separately and acoustic modes in the vertical are solved implicitly. For real cases on the globe, the Lambert map projection

> Triangular-based mesh



- > Actual **resolution** (square-based domain) is $\approx \frac{2}{3}dx$
- > All **variables** defined at triangle barycenters: T_{ij} B_{ij}
- > 1st **derivatives** (slopes) at T/B from neighbor B/T
- > 2nd **derivatives** (e.g. diffusion) using all four T/B

- > True 2D REA instead of dimensional splitting



- > MC Slope Limiter, using local and neighbor slopes

- > 6-cell average wind at corners $\bar{U}_{ij}^n$ $\bar{V}_{ij}^n$

- > Linear profile for wind within cell:
$$\begin{cases} x' = \bar{U}_{ij}^n + Ax + By \\ y' = \bar{V}_{ij}^n + Cx + Dy \end{cases}$$

Non-Hydrostatic Fully-Compressible Equations

> FINAL version of Euler (Navier-Stokes) equations

$$\frac{\partial \pi'}{\partial t} = -u \frac{\partial \pi'}{\partial x} - v \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R}{c_v} (\bar{\pi} + \pi') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right]$$

$$\frac{\partial \theta'}{\partial t} = -u \frac{\partial \theta'}{\partial x} - v \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} + \mu \left[\nabla^2 \theta' + \frac{\partial^2 (\bar{\theta} + \theta')}{\partial z^2} \right]$$

$$\frac{\partial u}{\partial t} = -u \frac{\partial u}{\partial x} - v \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial x} + f v - \hat{f} w + \mu \left[\nabla^2 u + \frac{\partial^2 u}{\partial z^2} \right]$$

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial x} - v \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial y} - f u + \mu \left[\nabla^2 v + \frac{\partial^2 v}{\partial z^2} \right]$$

$$\frac{\partial w}{\partial t} = -u \frac{\partial w}{\partial x} - v \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial z} + g \frac{\theta'}{\bar{\theta}} + \hat{f} u + \mu \left[\nabla^2 w + \frac{\partial^2 w}{\partial z^2} \right]$$

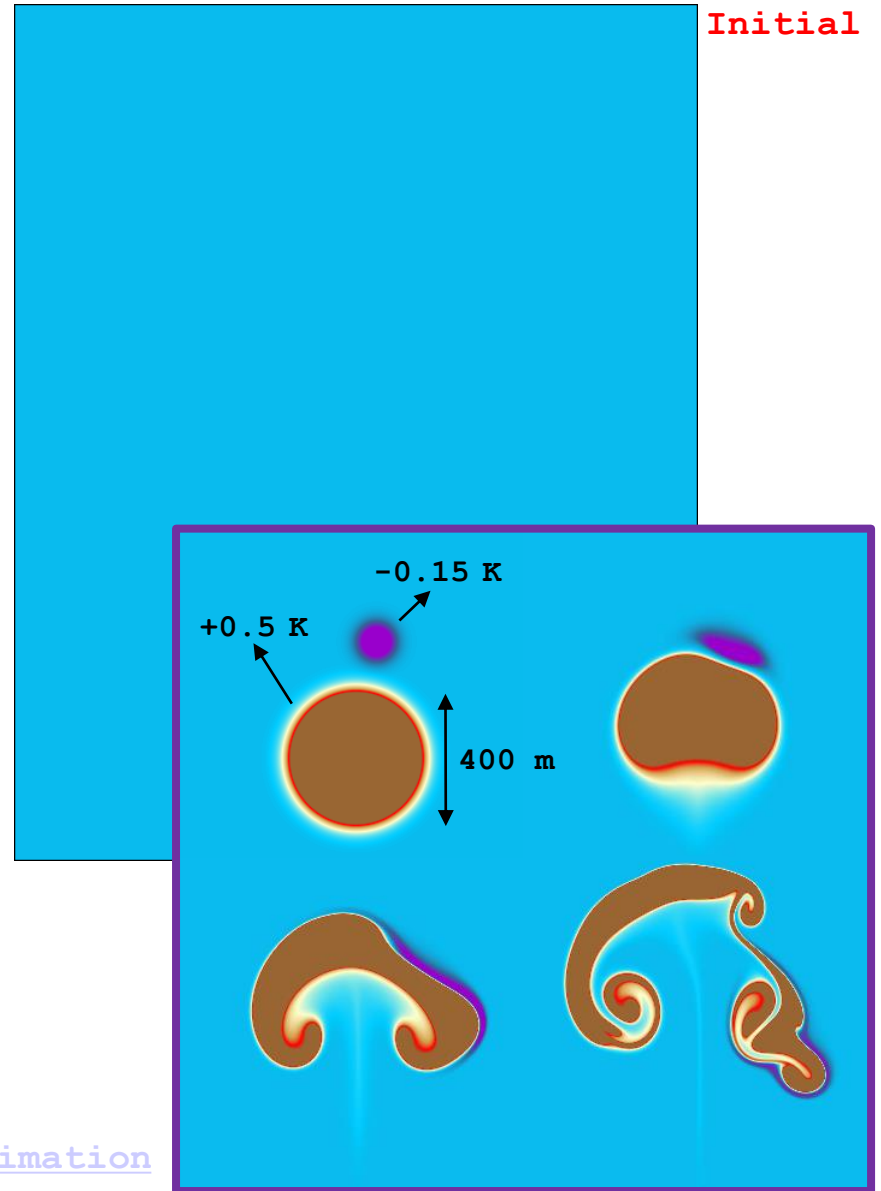
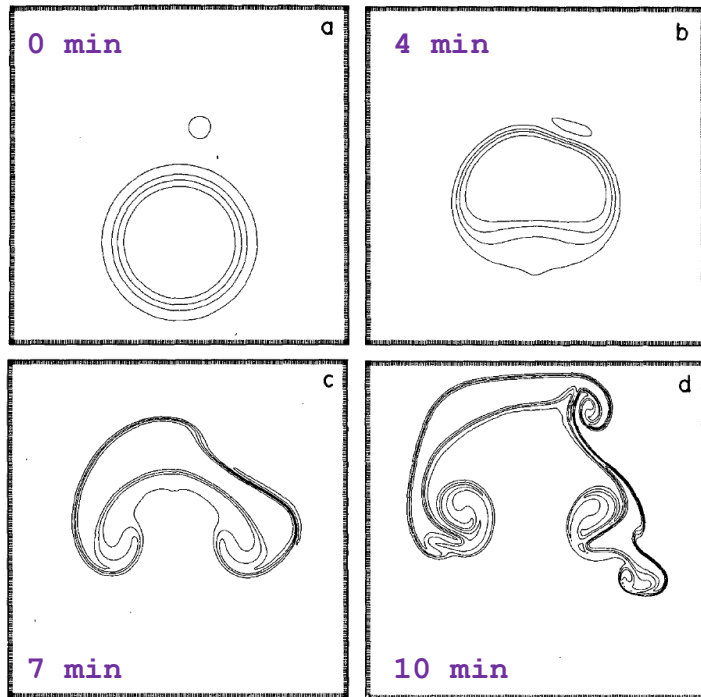
> Numerical implementation 3D [CFL $\xrightarrow{c_s > 300 \text{ m/s}}$ $\Delta t \approx 2 \Delta x(\Delta z)$]

- * Forward-Backward integration of "forcings" in RK2 cycle
- * REA (V and H) integration of advection every 6-10 Nsteps
- * Rigid Wall BCs at W/E S/N B/T boundaries

> Large Warm & Small Cold Bubbles

 $(dx=dz=2.5\text{m}, dt=0.00625\text{s}, N_{\text{step}}=10, 40\text{min})$

Robert (1993)

Animation

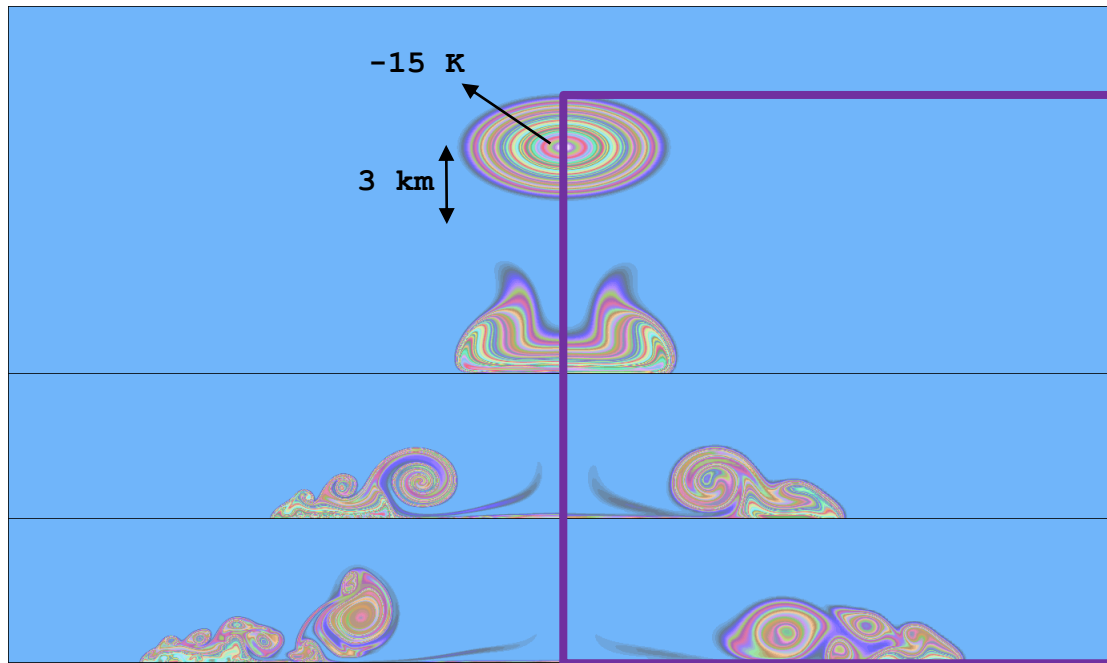
> Density Current

($dx=dz=100\text{m}$, $dt=0.25\text{s}$, $N_{\text{step}}=10$, **3h**)

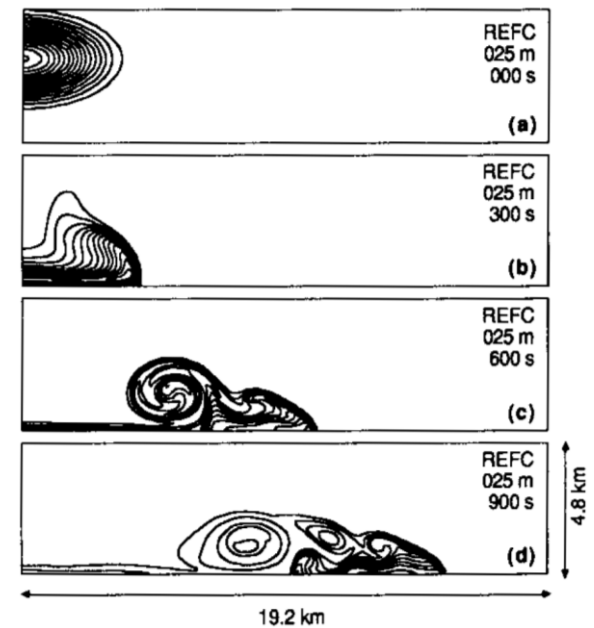


Quadruple resolution

Initial

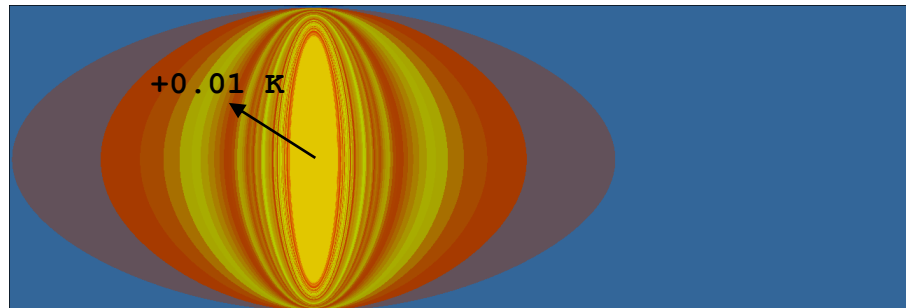


Straka et al. (1993)

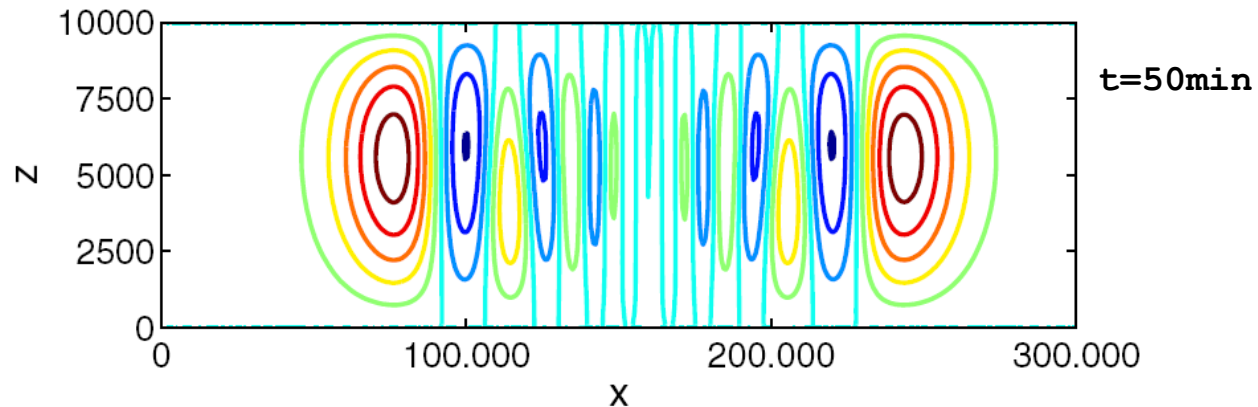


> Inertia-Gravity Waves (uniform wind/stability: $U=20\text{ms}^{-1}/N=0.01\text{s}^{-1}$)

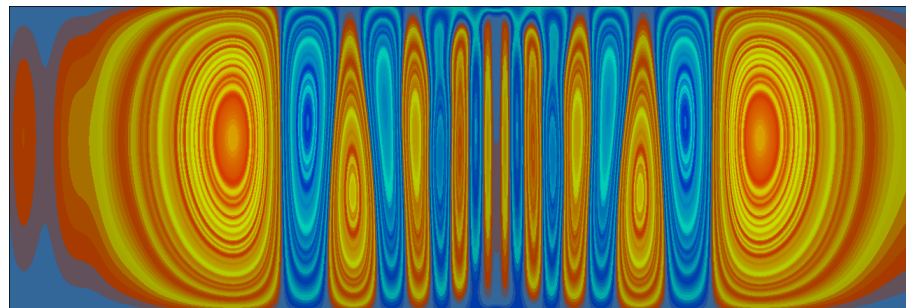
($dx=dz=125\text{m}$, $dt=0.3125\text{s}$, $N_{\text{step}}=10$, 1h)



Initial



Giraldo
&
Restelli
(2008)



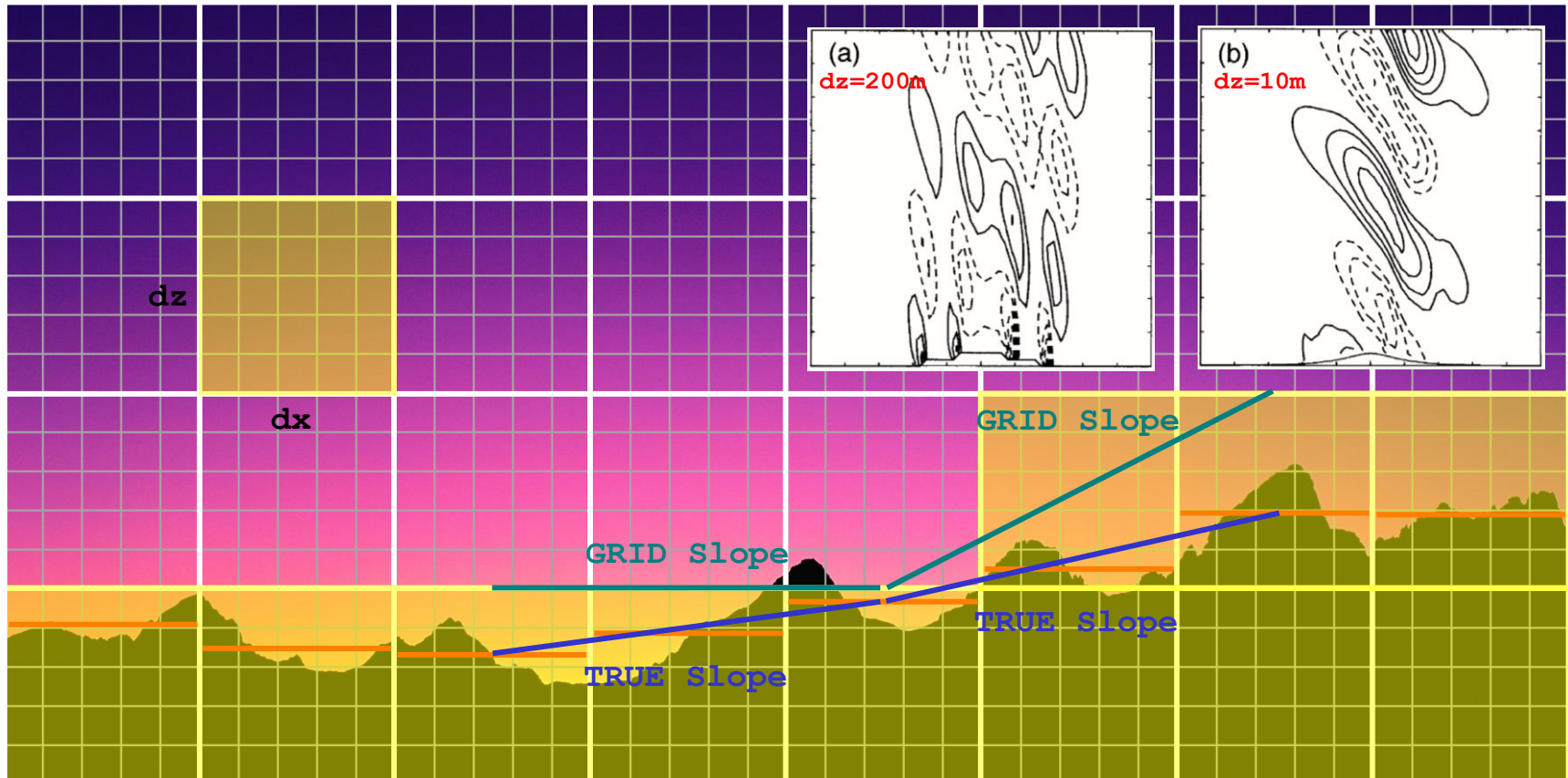
Animation

Inclusion of Orography (+ GW Absorbing Layer)

> TRUE-terrain slope vs GRID-based slope

ETA MODEL

Gallus & Klemp (2000)



NO forcing !!!

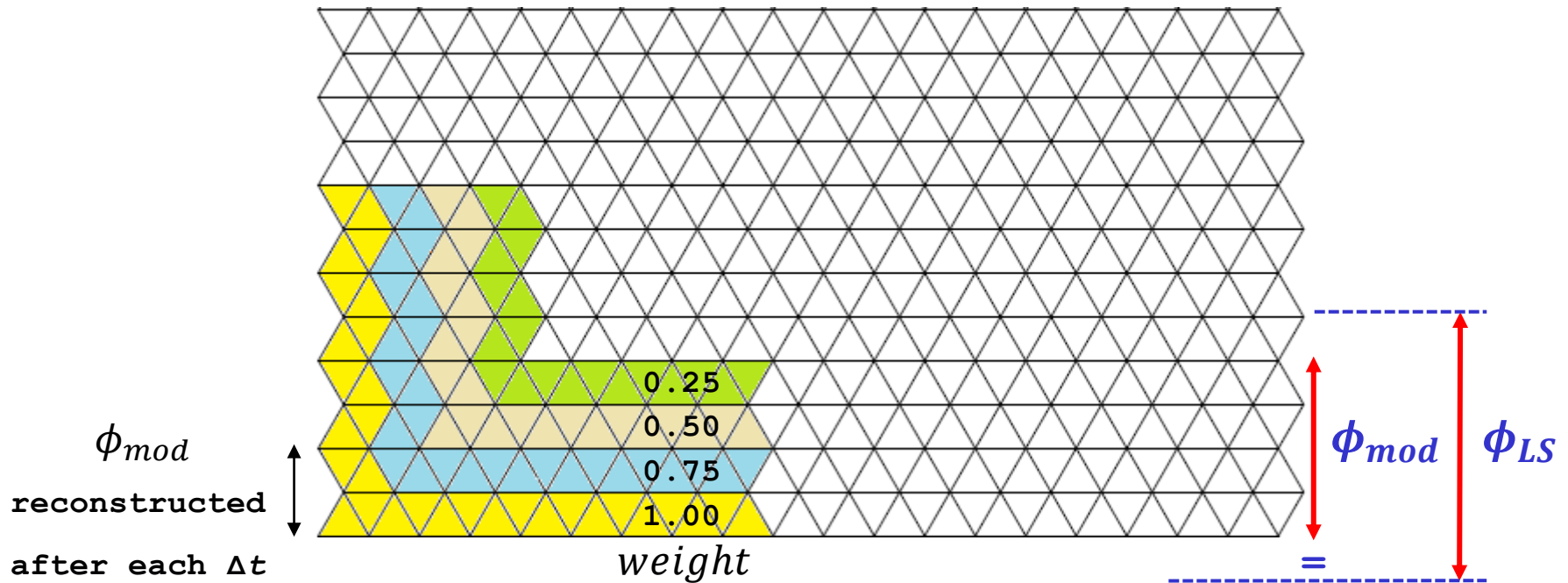
TOO MUCH forcing !!!

CORRECT forcing

CORRECT forcing

Specified Lateral Boundary Conditions

> Interior solution ϕ_{mod} relaxed towards specified ϕ_{LS}

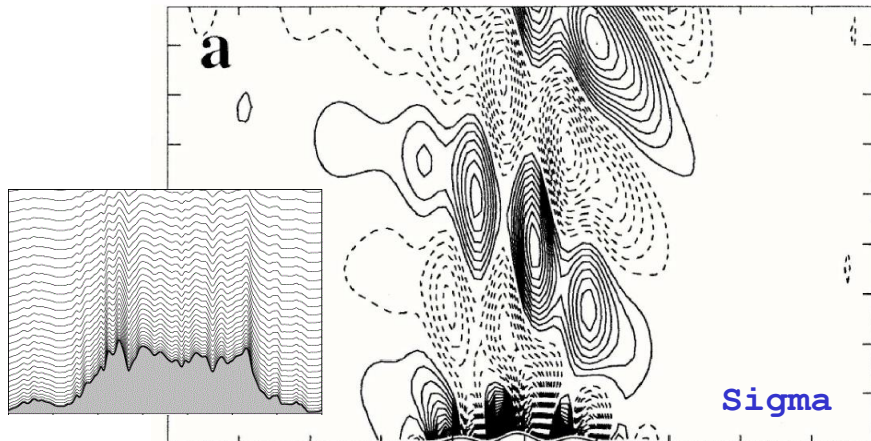


$$\frac{\partial \phi_{mod}}{\partial t} = \text{weight} [F(\phi_{LS} - \phi_{mod}) - G\Delta^2(\phi_{LS} - \phi_{mod})]$$

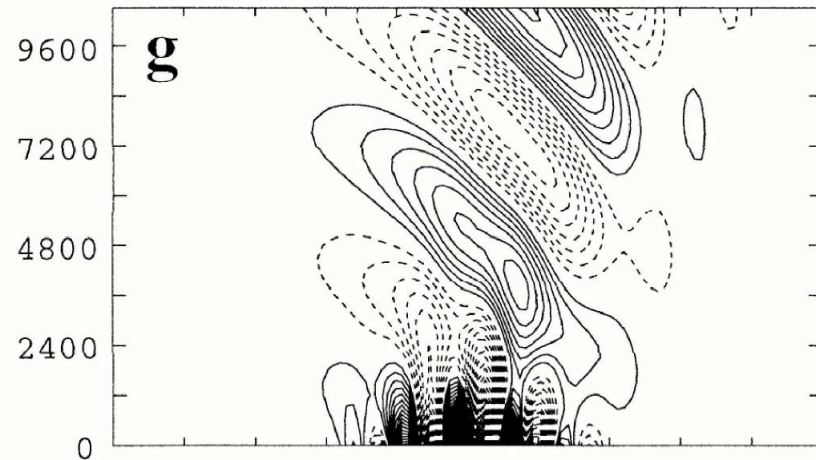
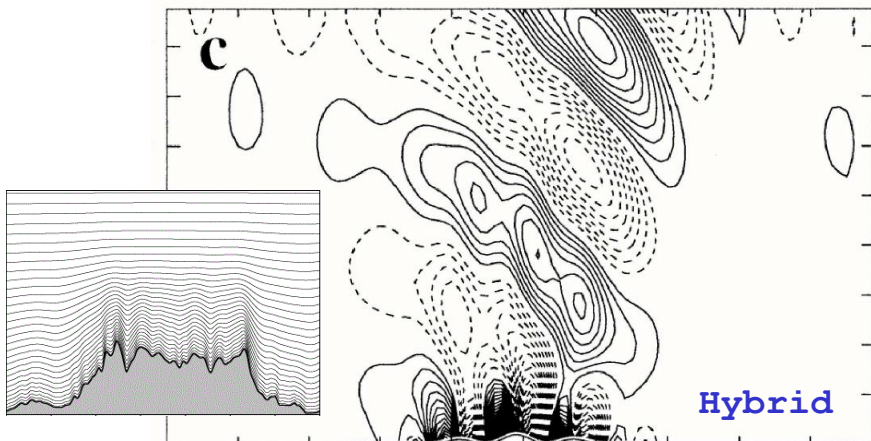
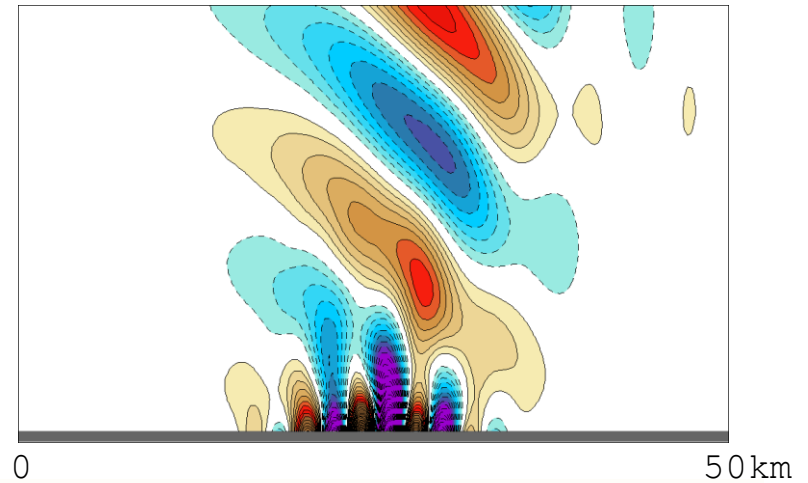
> Typical values $\begin{cases} F = 1/10\Delta t \\ G = 1/50\Delta t \end{cases}$ ($\times 5$ if using grid analyses)

> Schär Mountain (250m bell-shaped + small-scale, $U=10\text{ms}^{-1}$, $N=0.01\text{s}^{-1}$)

($dx=250\text{m}$, $dz=250\text{m}$, $dt=0.75\text{s}$, $N_{\text{step}}=10$, 10h)



Steady-state

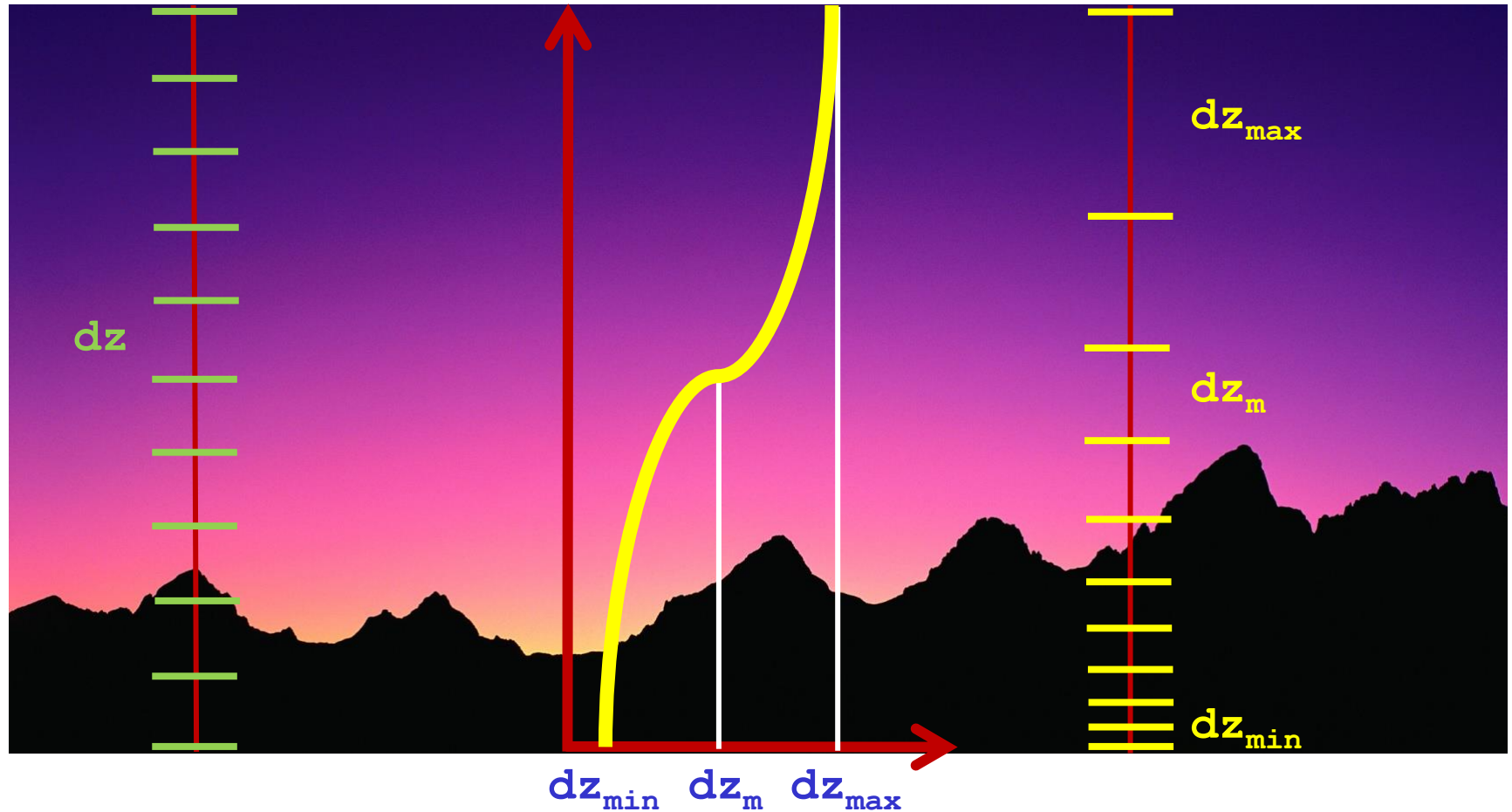


Schär et al. (2002)

Analytical

Vertical Stretching (+ Stabilization Fast Modes)

> Higher resolution at low levels (cos profile)



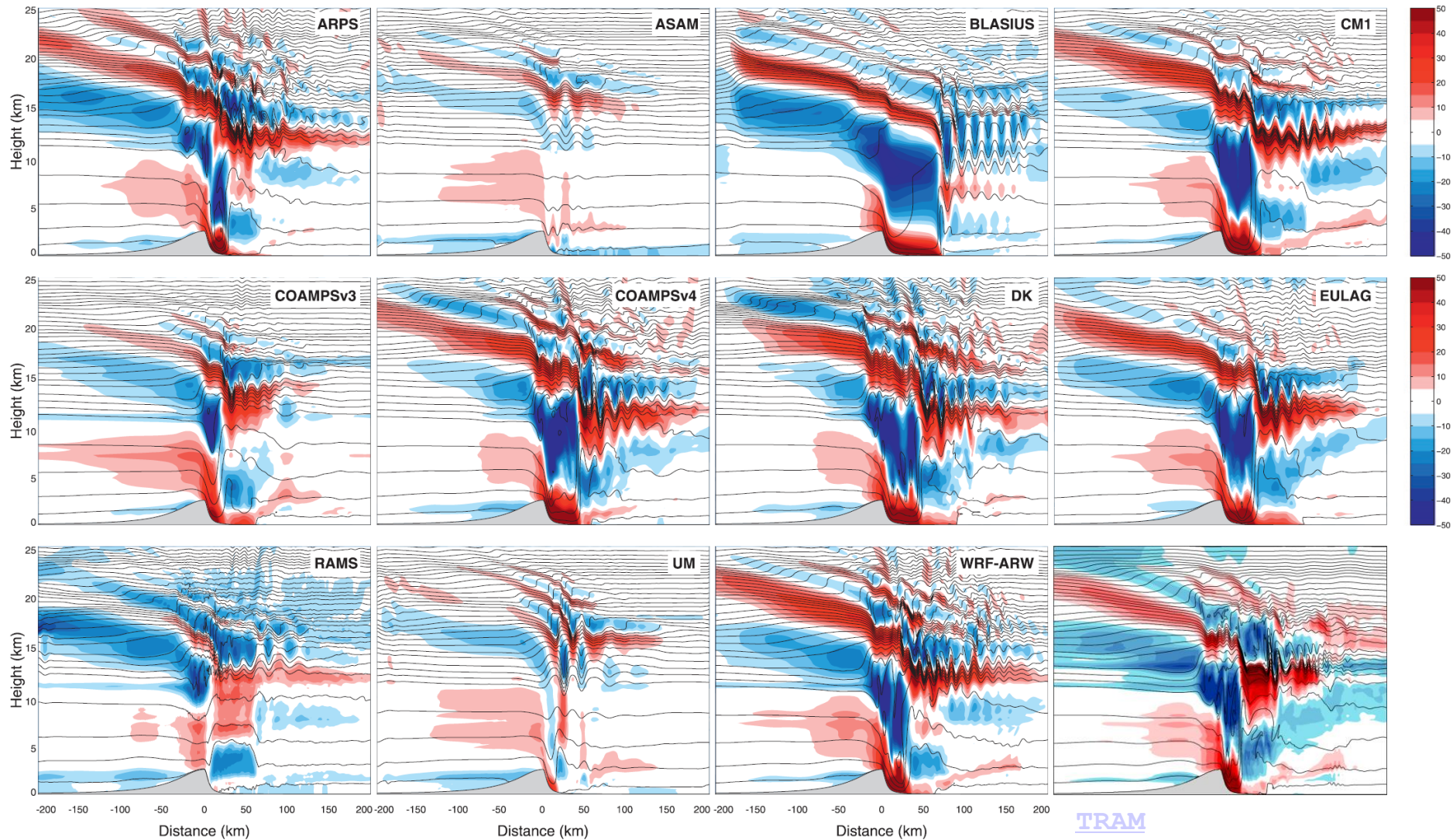
> Two parameters ($stretch, dz_m$) $\begin{cases} dz_{min} = dz_m / stretch \\ dz_{max} = dz_m + (dz_m - dz_{min}) \end{cases}$

> T-REX Intense Mountain-Wave

t=4h

(dx=500m,dzm=100m,stretch=5,dt=1.5s,Nstep=6,20h)

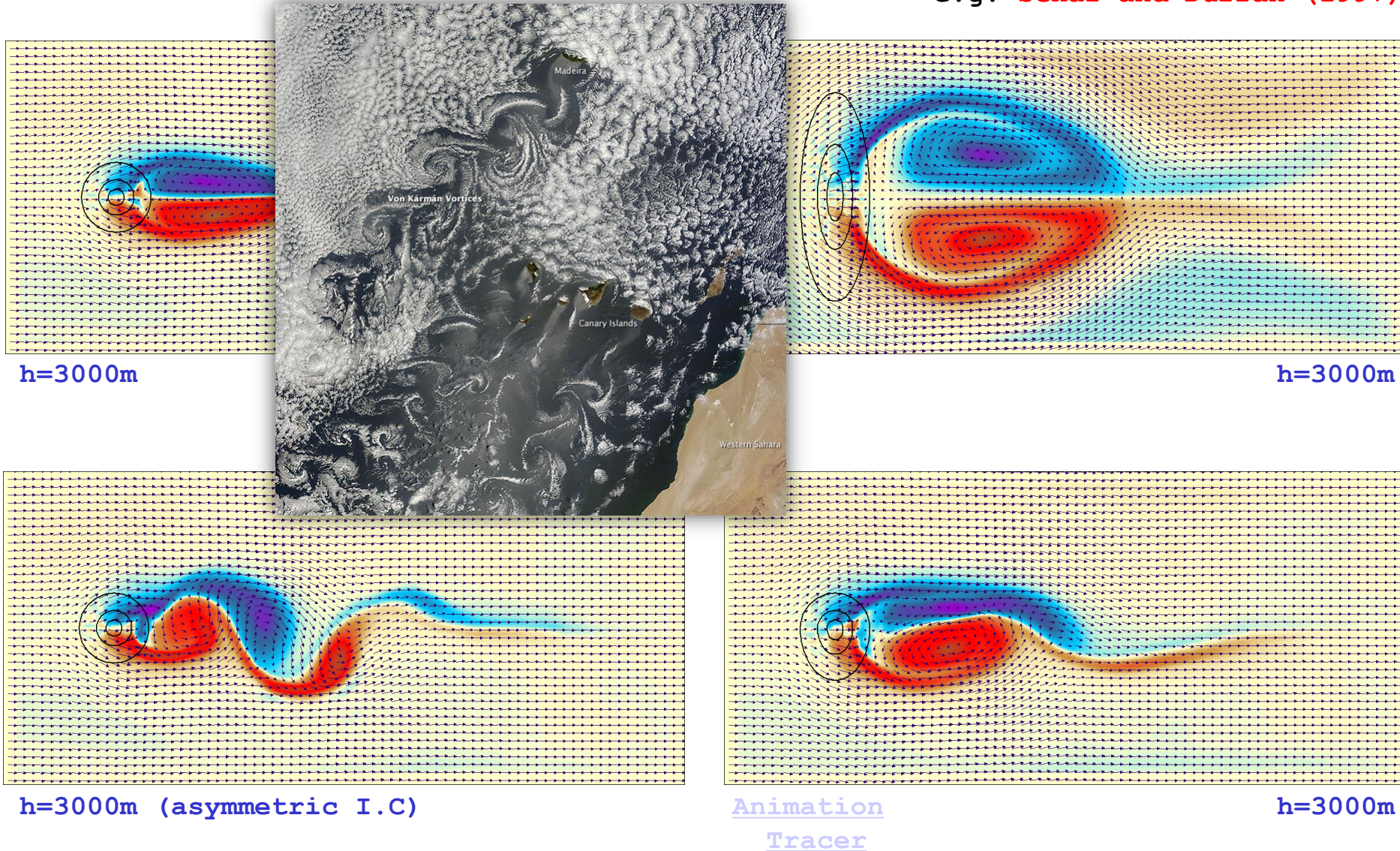
Doyle et al. (2011)



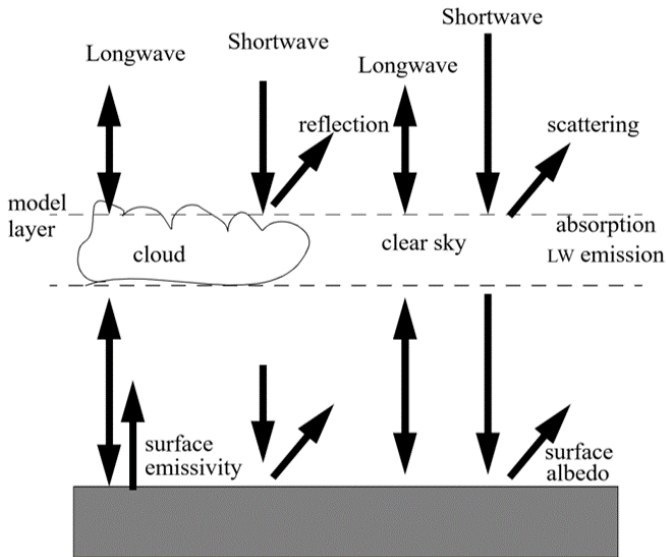
> Von Kármán Vortex Streets ($U=10\text{ms}^{-1}$, $N=0.01\text{s}^{-1}$)

(dx=2km,dzm=500m,stretch=2,dt=4s,Nstep=10,48h)

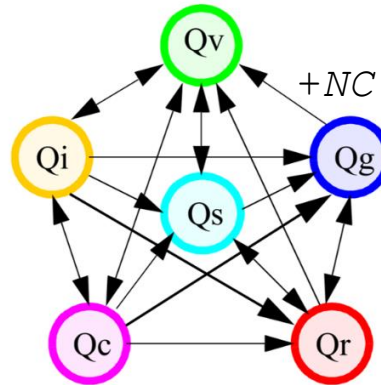
e.g. **Schär and Durran (1997)**



Radiation



Microphysics



NEW

Prognostic fields

$$Q_\chi$$

Forcing terms

$$F_{Q_\chi}$$

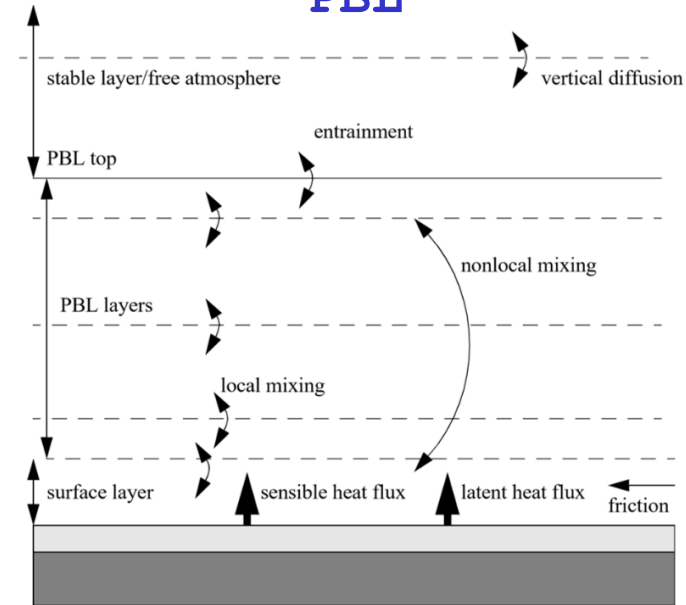
$$F_T$$

$$F_u \quad F_v$$

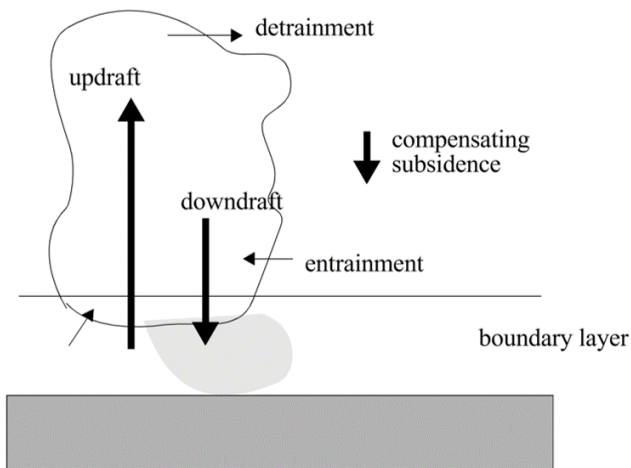
Surface variables

$$T_g \quad R_{nc} \quad R_c \quad \dots$$

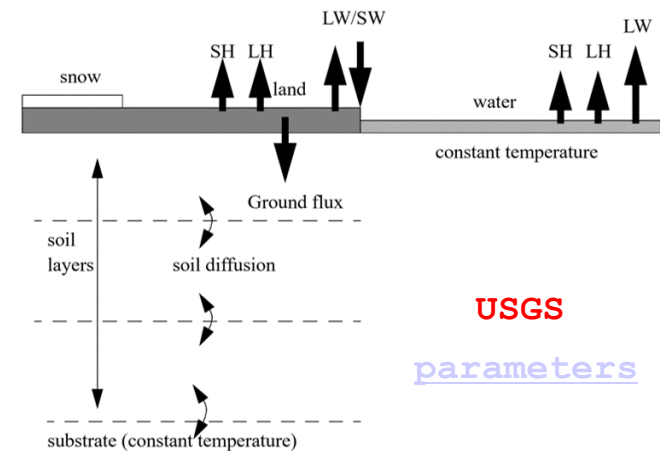
PBL



Cumulus



Surface



USGS

parameters

NEW Form of Equations: MESOSCALE-IDEALized

$$\frac{\partial \pi'}{\partial t} = -u \frac{\partial \pi'}{\partial x} - v \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right] + \frac{R_d}{c_{vm}} \frac{1}{\bar{\theta} + \theta'} \mathbf{E}_T$$

ALL moist effects on pressure and thermodynamics

$$+ \frac{R_d}{c_p} \frac{R_v}{R_m} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \mathbf{E}_{Q_v}$$

$$\frac{\partial \theta'}{\partial t} = -u \frac{\partial \theta'}{\partial x} - v \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} - \left(\frac{R_m}{c_{vm}} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} \right) (\bar{\theta} + \theta') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right]$$

Physics computed in NSTEP-cycle

$$+ \frac{c_v}{c_{vm}} \frac{1}{\bar{\pi} + \pi'} \mathbf{E}_T + \frac{R_v}{c_{vm}} \left(1 - \frac{R_d}{c_p} \frac{c_{pm}}{R_m} \right) (\bar{\theta} + \theta') \mathbf{E}_{Q_v}$$

$$\frac{\partial u}{\partial t} = -u \frac{\partial u}{\partial x} - v \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial x} + f v - \hat{f} w + \mathbf{E}_u$$

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial x} - v \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial y} - f u + \mathbf{E}_v$$

$$\pi = \left(\frac{P}{P_0} \right)^{R_d/c_p} \quad \theta = \frac{T}{\pi} \quad P = \rho R_d T^{\frac{1+Q_v/\varepsilon}{1+Q_v}}$$

$$\theta_\rho = \theta \frac{1+Q_v/\varepsilon}{1+Q_v+Q_{liq}+Q_{ice}} \quad c_p \bar{\theta}_\rho \frac{\partial \bar{\pi}}{\partial z} = -g$$

$$\frac{\partial w}{\partial t} = -u \frac{\partial w}{\partial x} - v \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial z} + g \frac{\theta'_\rho}{\bar{\theta}_\rho} + \hat{f} u - g(Q_{liq} + Q_{ice})$$

$$\frac{\partial Q_x}{\partial t} = -u \frac{\partial Q_x}{\partial x} - v \frac{\partial Q_x}{\partial y} - w \frac{\partial Q_x}{\partial z} + \mathbf{E}_{Q_x}$$

$$R_m = R_d + R_v \quad Q_v = \varepsilon = R_d / R_v$$

$$c_{pm} = c_p + c_{pv} \quad Q_v + c_l Q_{liq} + c_i Q_{ice}$$

$$c_{vm} = c_v + c_{vv} \quad Q_v + c_l Q_{liq} + c_i Q_{ice}$$

NEW Form of Equations: SYNOPTIC-REALcase

$$\frac{\partial \pi'}{\partial t} = -mu \frac{\partial \pi'}{\partial x} - mv \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \left[m^2 \left(\frac{\partial (\frac{u}{m})}{\partial x} + \frac{\partial (\frac{v}{m})}{\partial y} \right) + \frac{\partial w}{\partial z} \right] + \frac{R_d}{c_{vm}} \frac{1}{\bar{\theta} + \theta'} E_T + \frac{R_d}{c_p} \frac{R_v}{R_m} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') E_{Q_v}$$

ALL Coriolis and curvature terms

$$\frac{\partial \theta'}{\partial t} = -mu \frac{\partial \theta'}{\partial x} - mv \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} - \left(\frac{R_m}{c_{vm}} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} \right) (\bar{\theta} + \theta') \left[m^2 \left(\frac{\partial (\frac{u}{m})}{\partial x} + \frac{\partial (\frac{v}{m})}{\partial y} \right) + \frac{\partial w}{\partial z} \right] + \frac{c_v}{c_{vm}} \frac{1}{\bar{\pi} + \pi'} E_T + \frac{R_v}{c_{vm}} \left(1 - \frac{R_d}{c_p} \frac{c_{pm}}{R_m} \right) (\bar{\theta} + \theta') E_{Q_v}$$

LAMBERT projection

$$\frac{\partial u}{\partial t} = -mu \frac{\partial u}{\partial x} - mv \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) m \frac{\partial \pi'}{\partial x} + v \left(f + u \frac{\partial m}{\partial y} - v \frac{\partial m}{\partial x} \right) - \hat{f} w \cos \alpha - \frac{uw}{a} + E_u$$

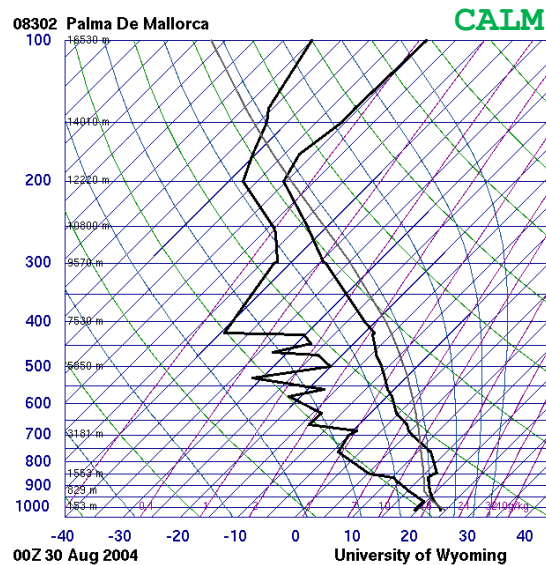
$$\frac{\partial v}{\partial t} = -mu \frac{\partial v}{\partial x} - mv \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) m \frac{\partial \pi'}{\partial y} - u \left(f + u \frac{\partial m}{\partial y} - v \frac{\partial m}{\partial x} \right) + \hat{f} w \sin \alpha - \frac{uw}{a} + E_v$$

$$\frac{\partial w}{\partial t} = -mu \frac{\partial w}{\partial x} - mv \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial z} + g \frac{\theta'_\rho}{\bar{\theta}_\rho} + \hat{f} (u \cos \alpha - v \sin \alpha) + \frac{u^2 + v^2}{a} - g(Q_{liq} + Q_{ice})$$

$$\frac{\partial Q_x}{\partial t} = -mu \frac{\partial Q_x}{\partial x} - mv \frac{\partial Q_x}{\partial y} - w \frac{\partial Q_x}{\partial z} + E_{Q_x}$$

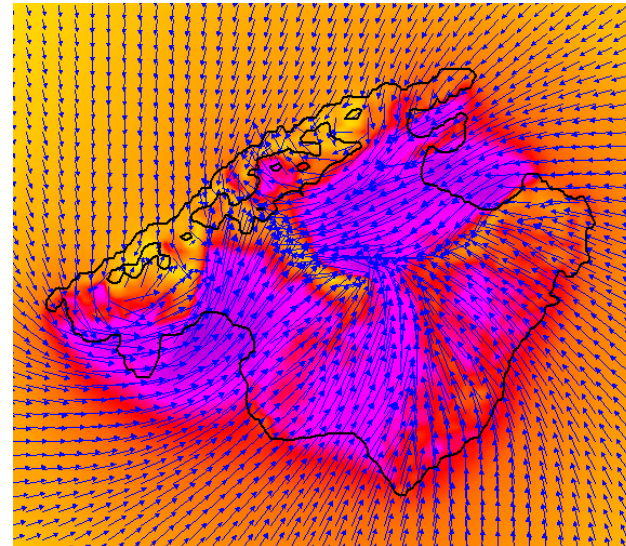
> Breeze Circulation in Mallorca (IC: Sounding 00 UTC 30 Ago 2004)

(dx=1.5km,dzm=400m,stretch=20,dt=3s,Nstep=10,30h)



m/s

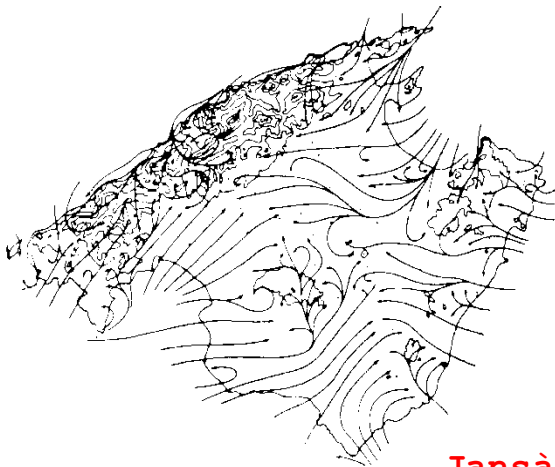
Run



t=13h

Clouds

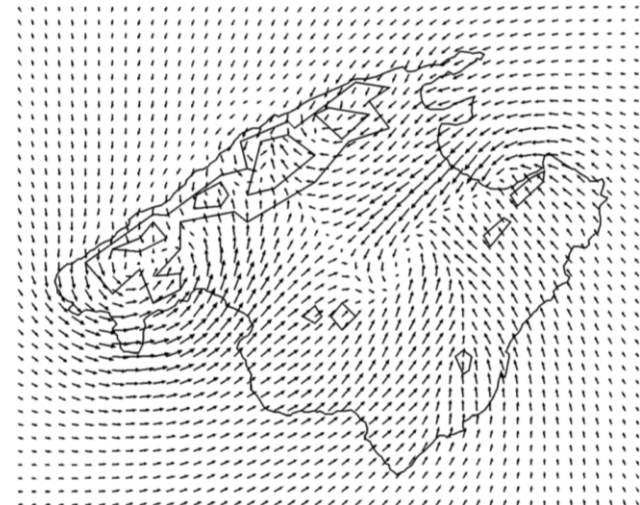
Rainfall



Jansà & Jaume (1946)

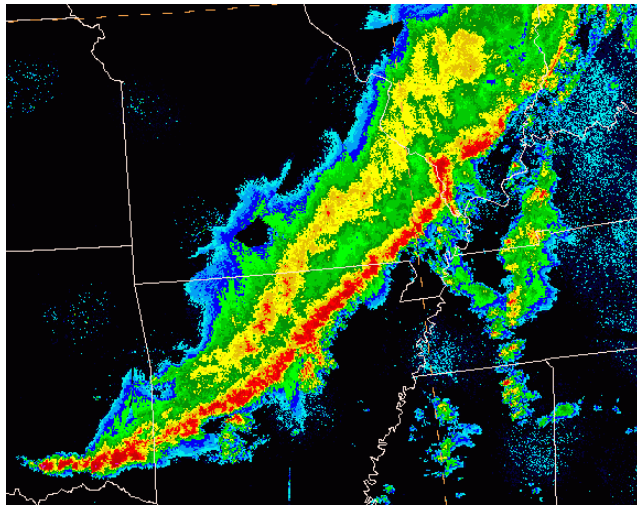


Ramis & Romero (1995)



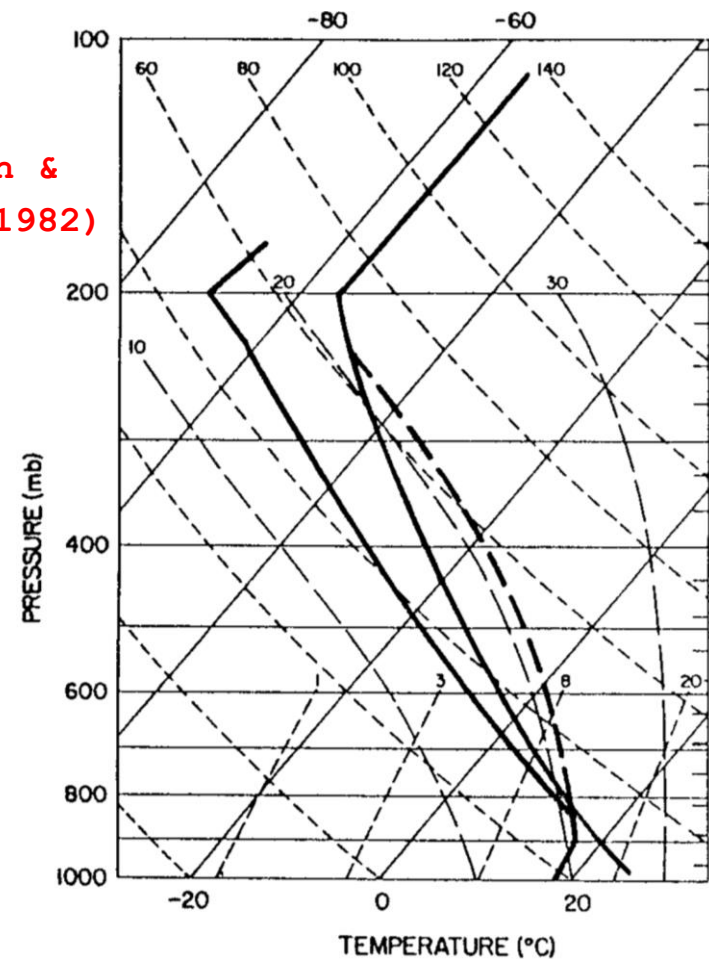
> Squall-Line Simulation (NO Coriolis, Radiation, PBL and Cumulus)

(dx=1.5km,dzm=200m,stretch=10,dt=3s,Nstep=5,10h)



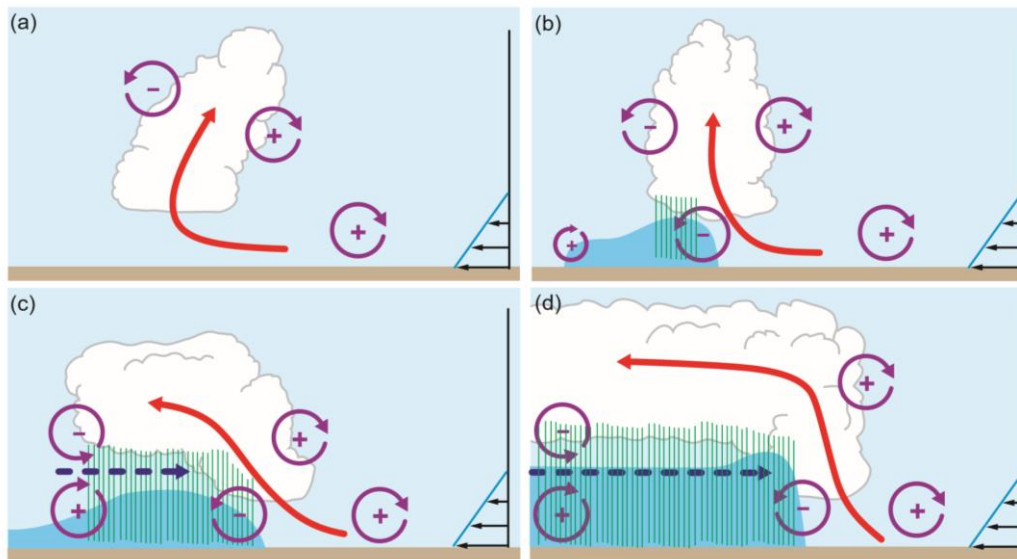
IC: WK82 SOUNDING + 8K Surface Cold Pool
... and 3 different wind profiles

Weisman &
Klemp (1982)



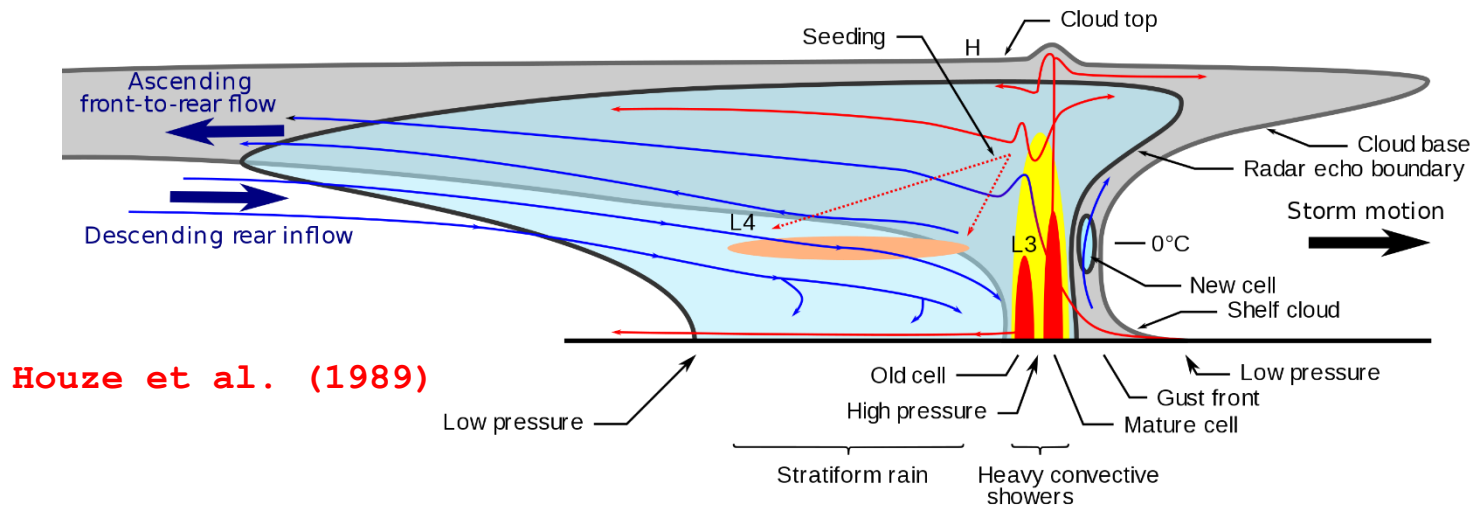
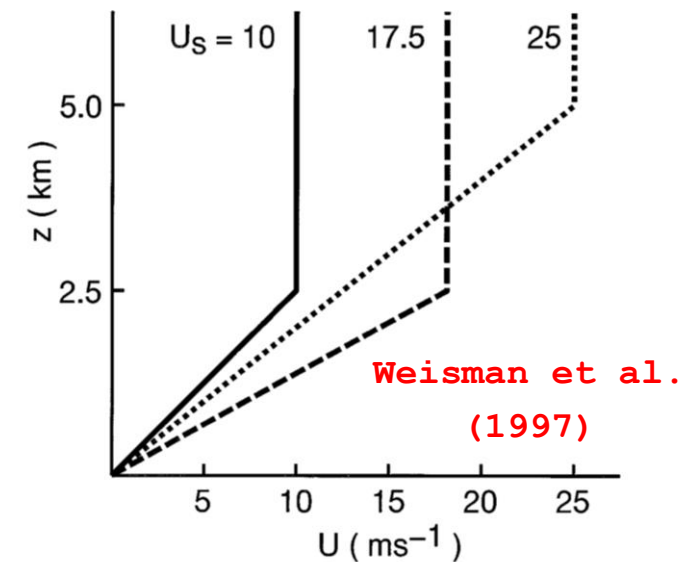
> Squall-Line Simulation (NO Coriolis, Radiation, PBL and Cumulus)

($dx=1.5\text{km}$, $dzm=200\text{m}$, $stretch=10$, $dt=3\text{s}$, $Nstep=5$, 10h)



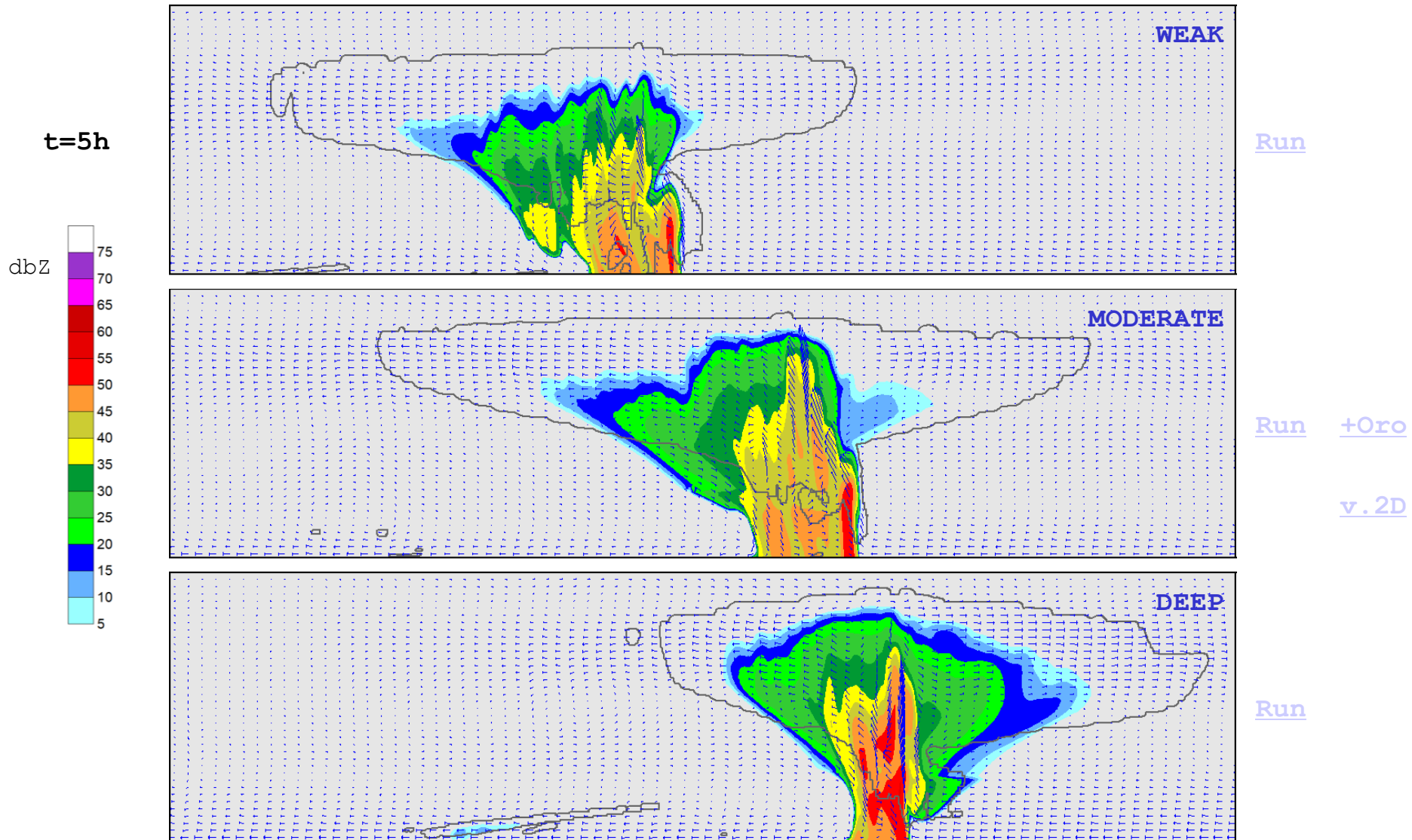
Weisman (1993)

SHEAR: Weak Moderate Deep



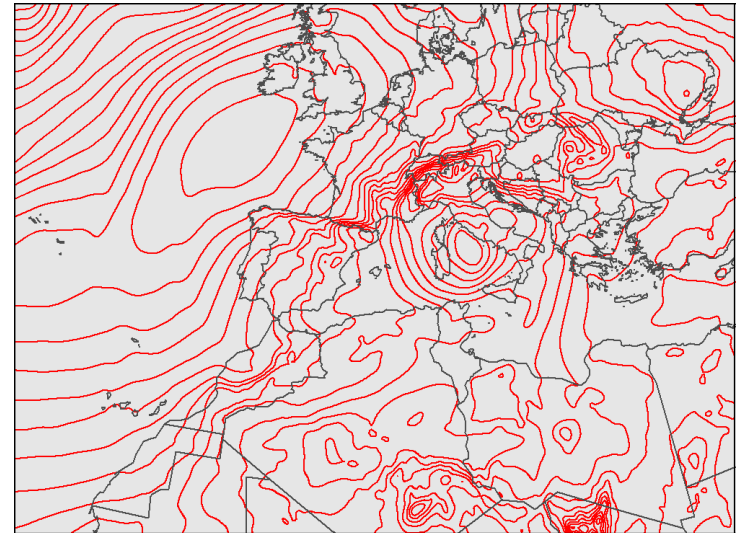
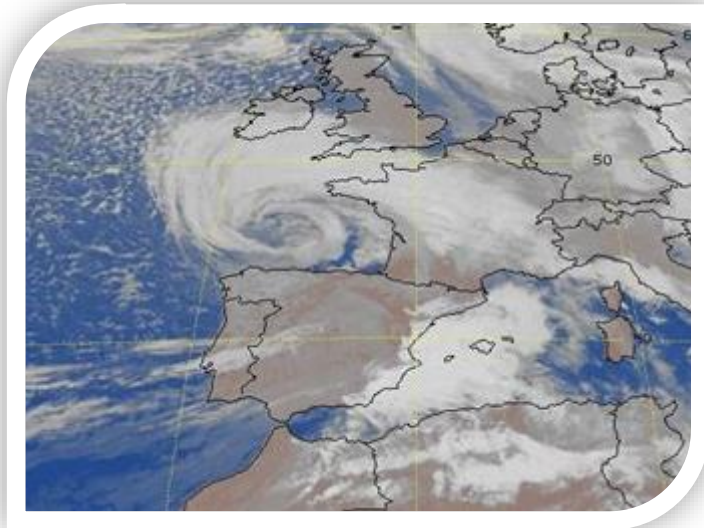
> Squall-Line Simulation (NO Coriolis, Radiation, PBL and Cumulus)

(dx=1.5km,dzm=200m,stretch=10,dt=3s,Nstep=5,10h)

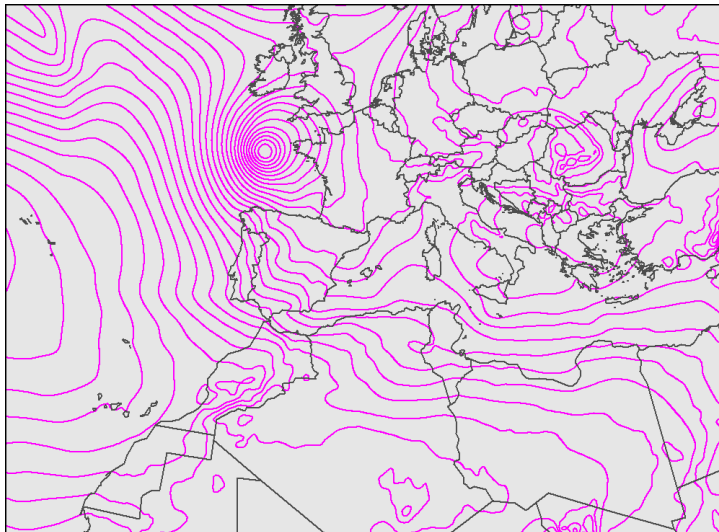


> "HUGO" Intense Cyclonic Storm (IC: 00 UTC 21 Mar 2018)

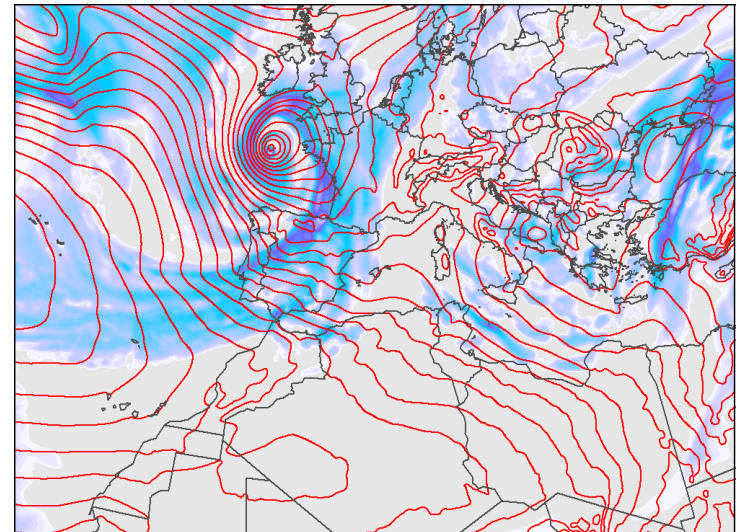
(MR: dx=25km, dzm=200m, stretch=10, dt=45s, Nstep=5, 90h)



t=0h



t=72h



kg/m²

4
3.6
3.2
2.8
2.4
2
1.6
1.2
0.8
0.4
0

ERA-5

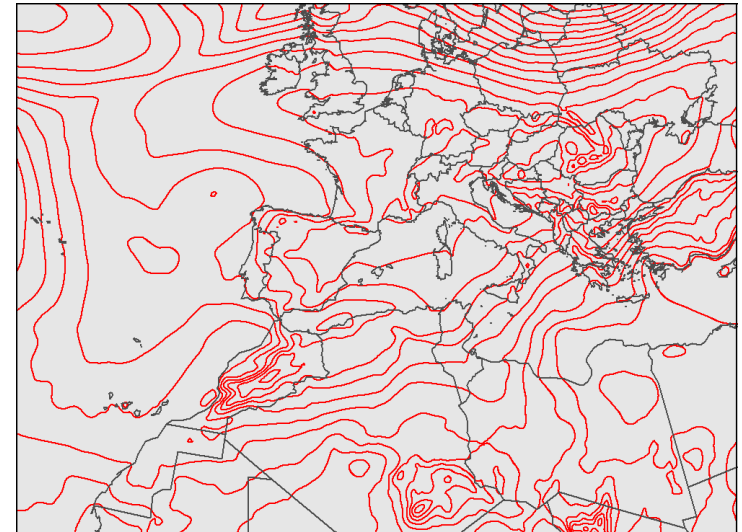
TRAM

Winds

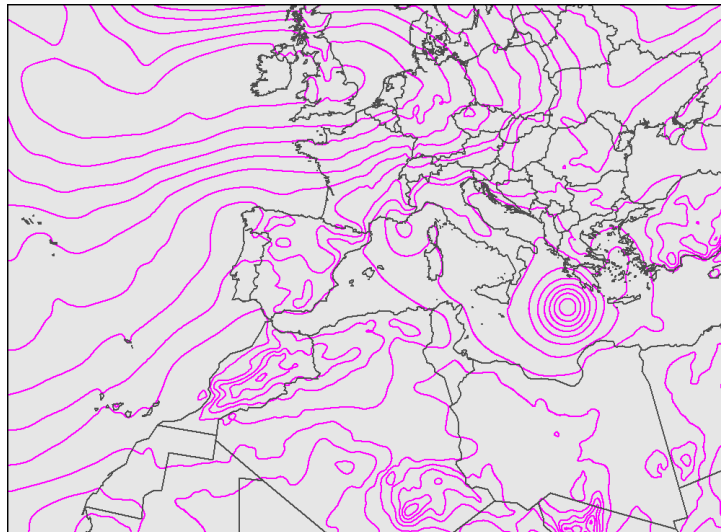
Rainfall

> "ZORBAS" Ionian Sea Medicane (IC: 00 UTC 27 Sept 2018)

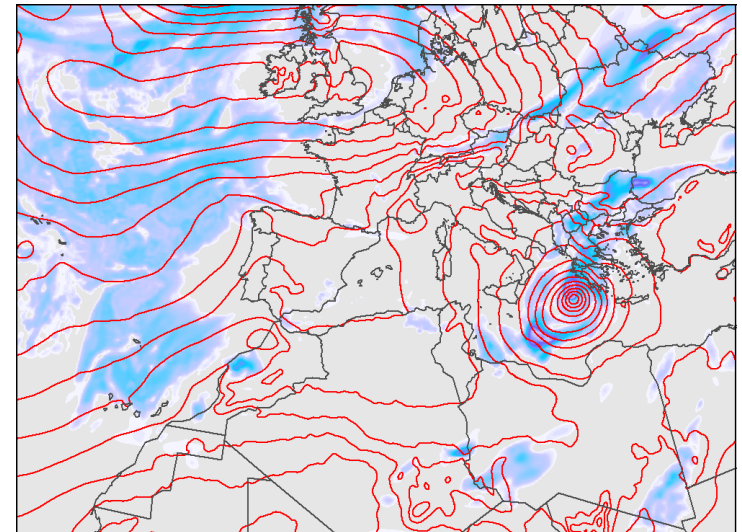
(MR: dx=25km, dzm=200m, stretch=10, dt=45s, Nstep=5, 90h)



t=0h



t=48h



kg/m²



ERA-5

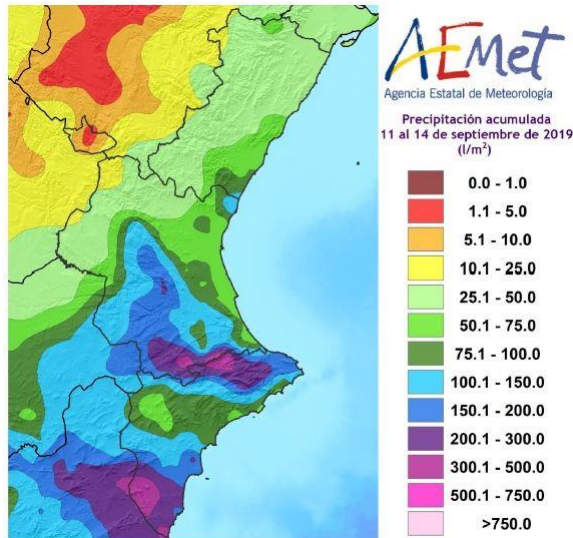
TRAM

Winds

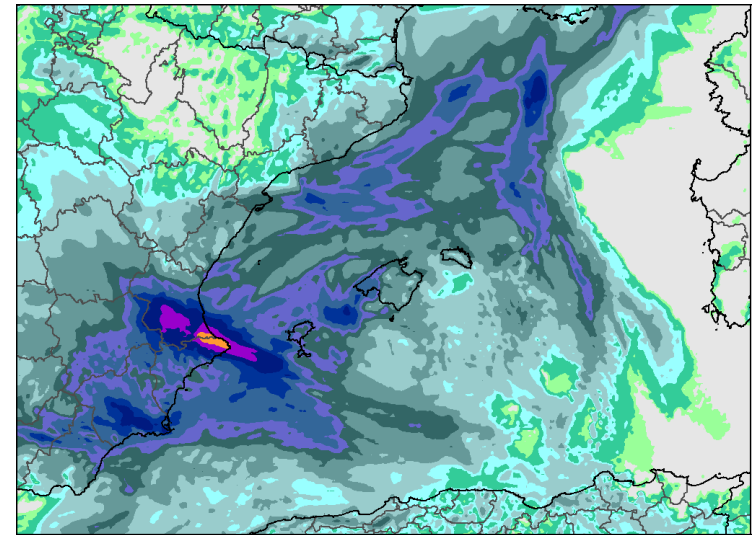
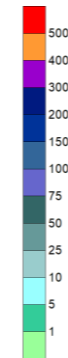
Rainfall

> "DANA" Valencia-Murcia Floods (IC: 00 UTC 10 Sept 2019)

(**HR_double**: dx=4.5km, dzm=200m, stretch=10, dt=9s, Nstep=5, **90h**)



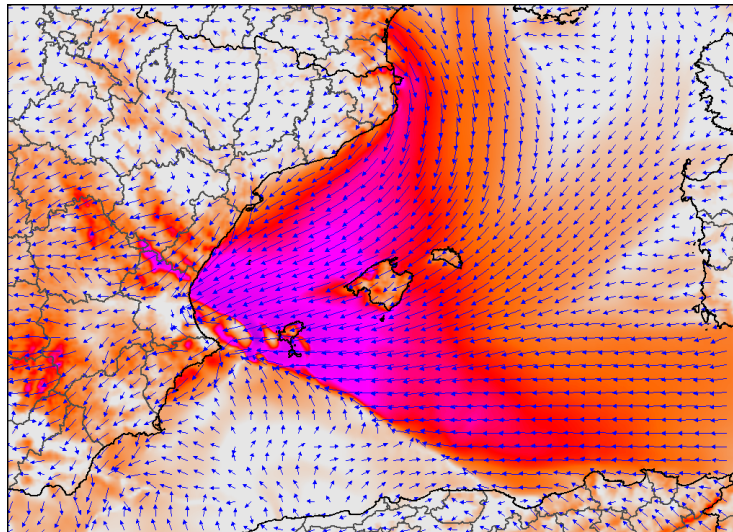
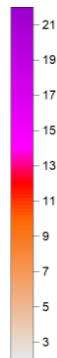
mm



total

Run

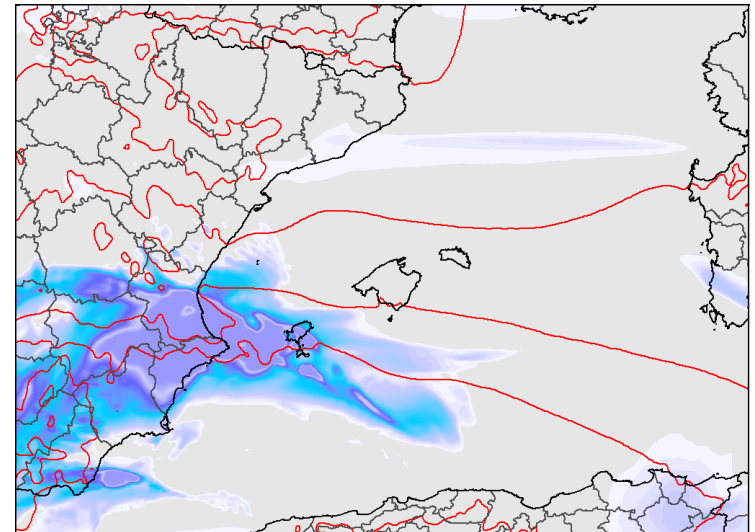
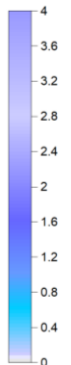
m/s



t=54h

Run

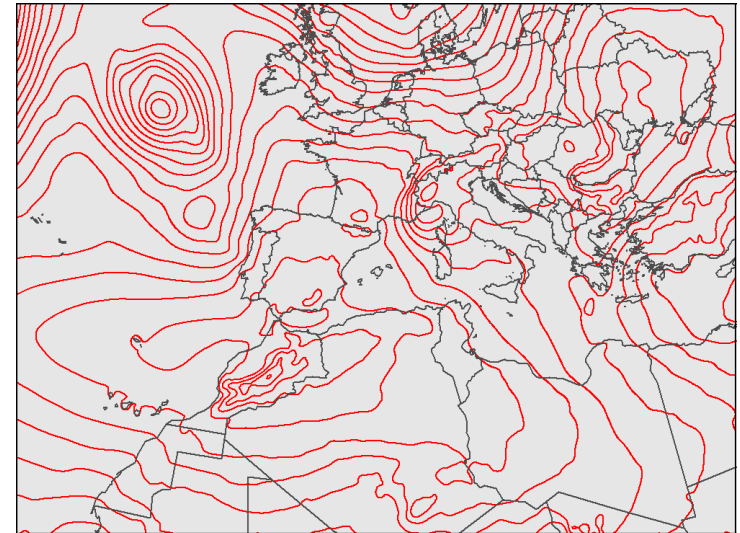
kg/m²



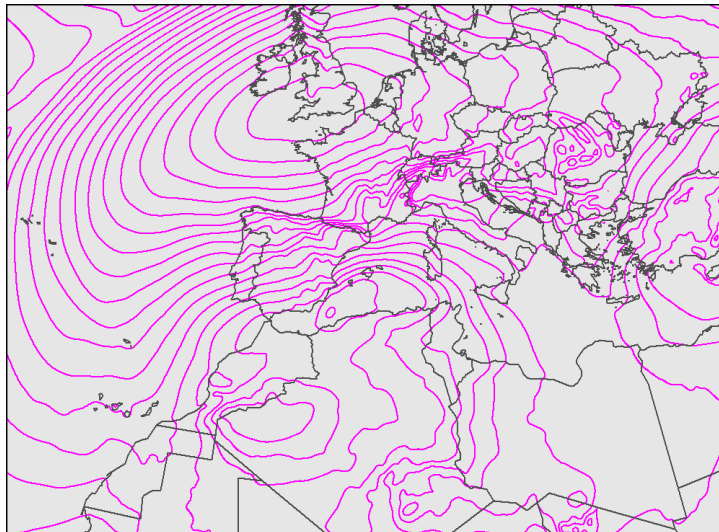
Run

> "GLORIA" Extraordinary Storm (IC: 00 UTC 18 Jan 2020)

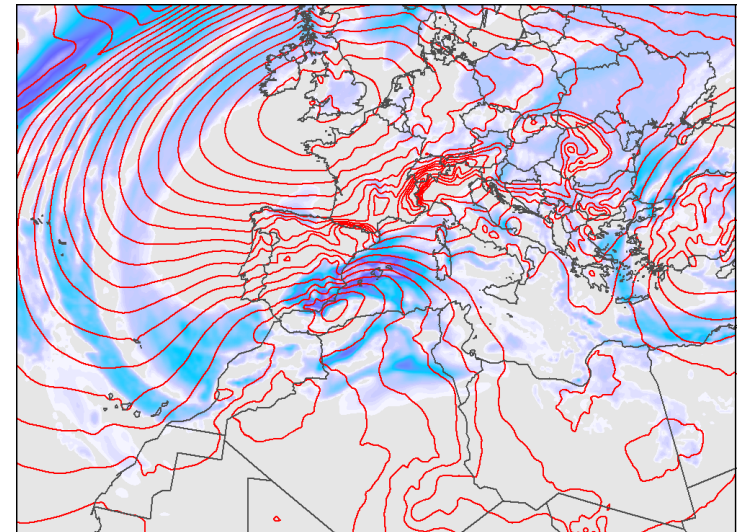
(MR: dx=25km, dzm=200m, stretch=10, dt=45s, Nstep=5, 138h)



t=0h



t=48h



kg/m²



ERA-5

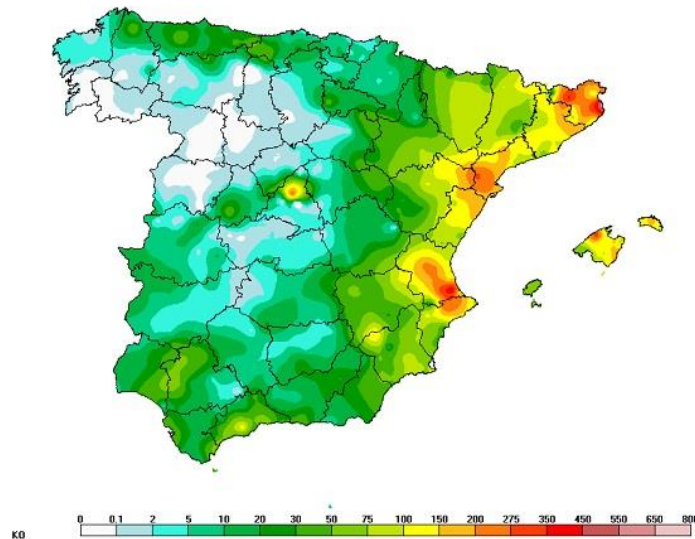
TRAM

Winds

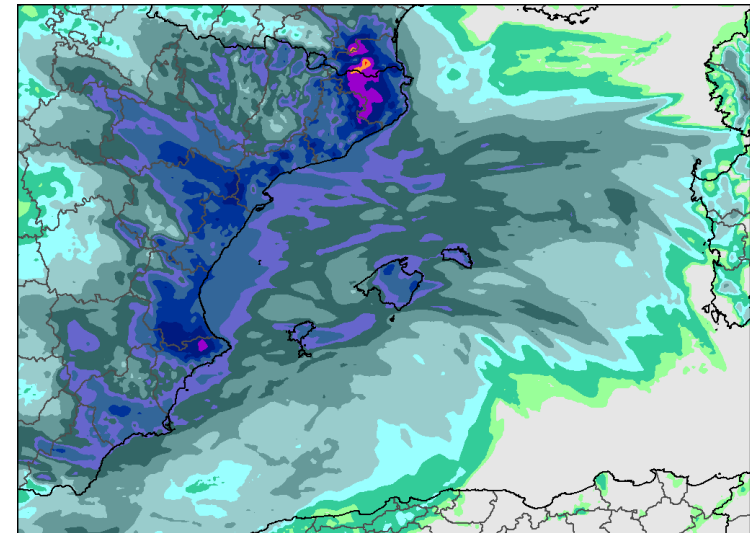
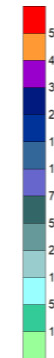
Rainfall

> "GLORIA" Extraordinary Storm (IC: 00 UTC 18 Jan 2020)

(HR_double: dx=4.5km, dzm=200m, stretch=10, dt=9s, Nstep=6, 138h)



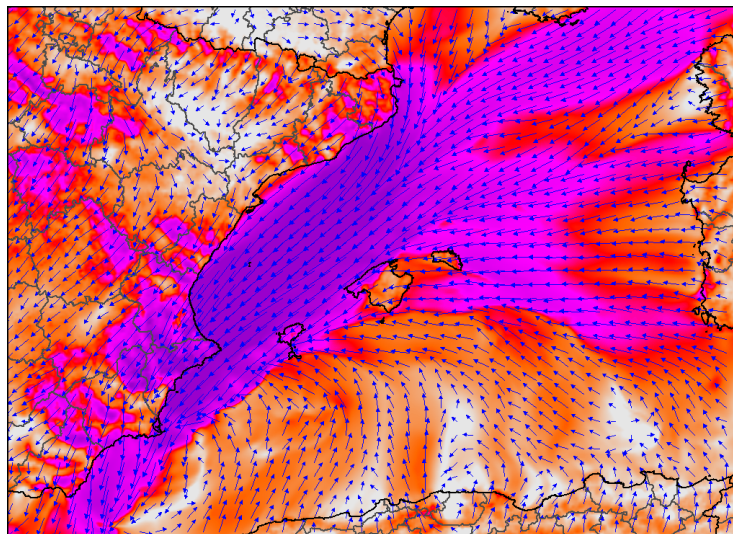
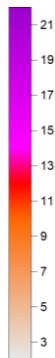
mm



total

Run

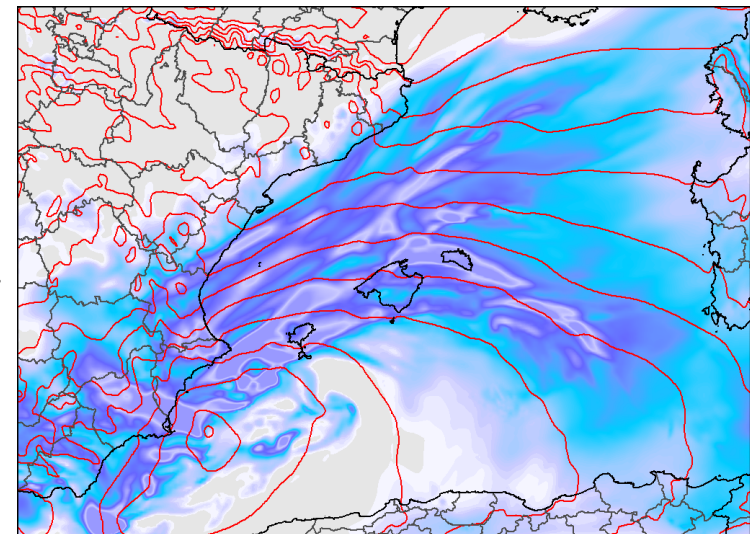
m/s



t=48h

Run

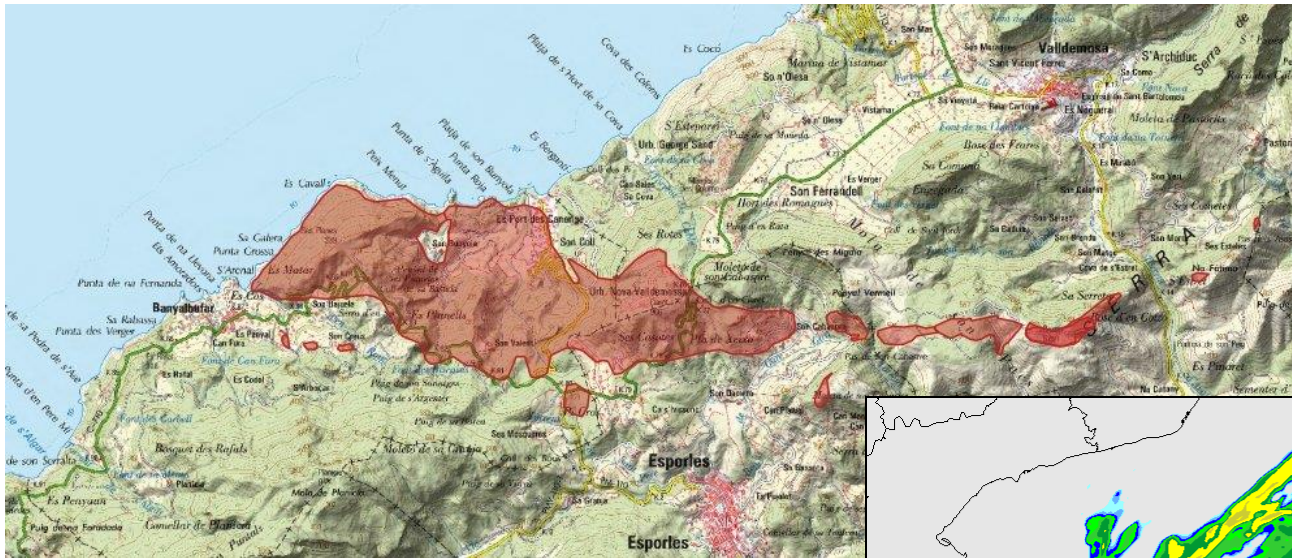
kg/m²



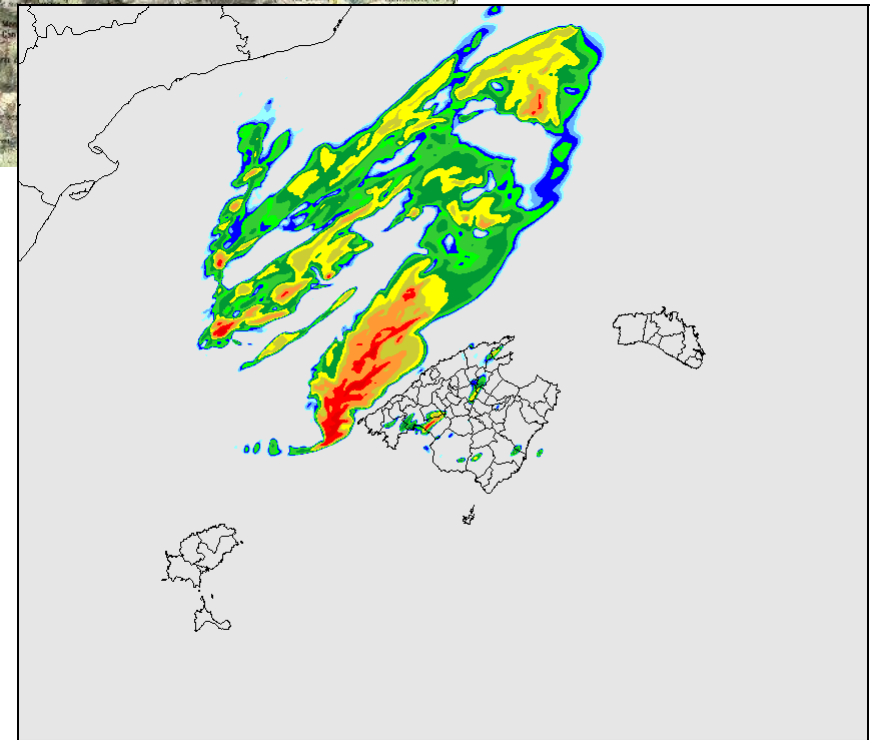
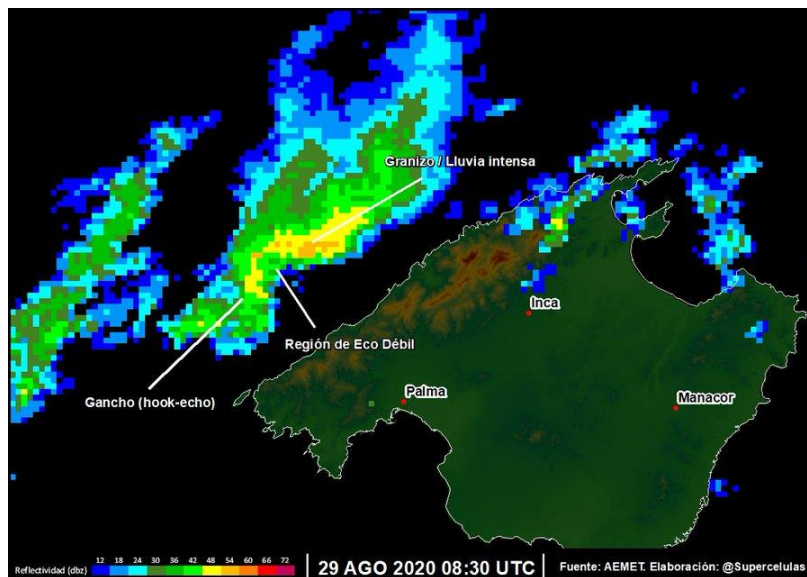
Run

BANYALBUFAR-ESPORLES Severe Supercell (29 August 2020)

> 29/00-29/18 **TRAM Simulation** (dx=0.75km, GFS-fcst)



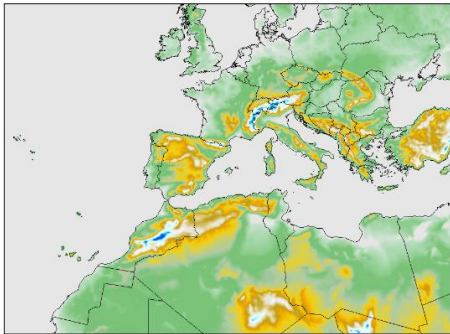
Run



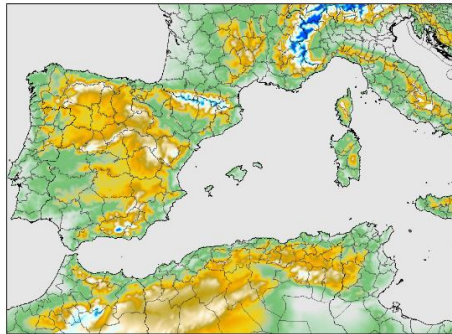
Wind Speed Rainfall Temperature

TRAM / MeteoUIB

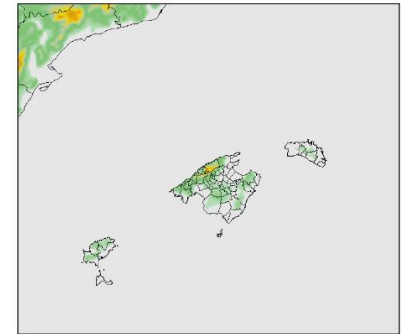
MR (17 km)



HR (6 km)



SR (2 km)



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THANK YOU
for
your attention