



Universitat
de les Illes Balears



The New *TRAM MODEL*:

*Achievements at Meteo-UIB Towards
Numerical Modelling Capabilities Aimed at a
Wide Range of Time-Space Scales*

Romu Romero

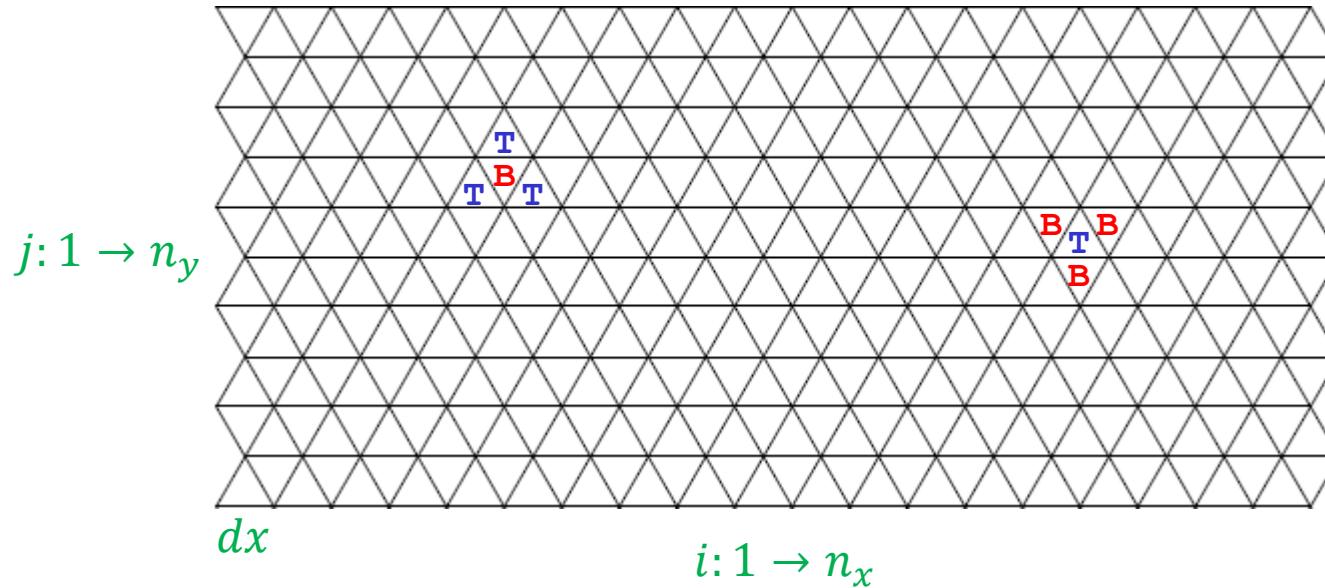
9th METMED Conference

Genoa (Italy), 22-24 May 2023

TRAM: Triangle-based Regional Atmospheric Model

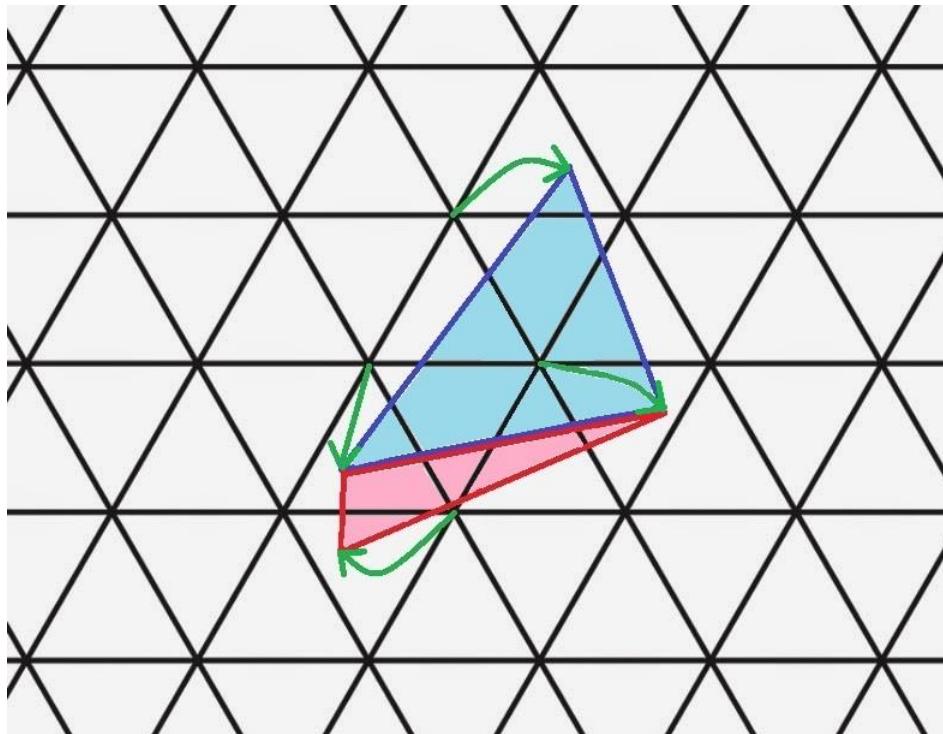
- > 16th EGU PLINIUS Conference (Montpellier, 2018):
“TRAM: A new nonhydrostatic fully compressible numerical model”
- > 7th METMED Conference (Palma de Mallorca, 2019):
“A computationally cheap atmosphere-ocean modelling system aimed at anticipating meteotsunami occurrence in Ciutadella”
- > 8th METMED Conference (Online, 2021):
“TRAM with physics: A new numerical model suited for all kinds of atmospheric applications”

> Triangular-based mesh



- > Actual **resolution** (square-based domain) is $\approx \frac{2}{3} dx$
- > All **variables** defined at triangle barycenters: T_{ij} B_{ij}
- > 1st derivatives (slopes) at T/B from neighbor B/T
- > 2nd derivatives (e.g. diffusion) using all four T/B

> True 2D REA instead of dimensional splitting



> MC Slope Limiter, using local and neighbor slopes

> 6-cell average wind at corners $\bar{U}_{ij}^n \bar{V}_{ij}^n$

> Linear profile for wind within cell: $\begin{cases} x' = \bar{U}_{ij}^n + Ax + By \\ y' = \bar{V}_{ij}^n + Cx + Dy \end{cases}$

Non-Hydrostatic Fully-Compressible Equations

> FINAL version of Euler (Navier-Stokes) equations

$$\frac{\partial \pi'}{\partial t} = -u \frac{\partial \pi'}{\partial x} - v \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R}{c_v} (\bar{\pi} + \pi') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right]$$

$$\frac{\partial \theta'}{\partial t} = -u \frac{\partial \theta'}{\partial x} - v \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} + \mu \left[\nabla^2 \theta' + \frac{\partial^2 (\bar{\theta} + \theta')}{\partial z^2} \right]$$

$$\frac{\partial u}{\partial t} = -u \frac{\partial u}{\partial x} - v \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial x} + fv - \hat{f}w + \mu \left[\nabla^2 u + \frac{\partial^2 u}{\partial z^2} \right]$$

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial x} - v \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial y} - fu + \mu \left[\nabla^2 v + \frac{\partial^2 v}{\partial z^2} \right]$$

$$\frac{\partial w}{\partial t} = -u \frac{\partial w}{\partial x} - v \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta} + \theta') \frac{\partial \pi'}{\partial z} + g \frac{\theta'}{\bar{\theta}} + \hat{f}u + \mu \left[\nabla^2 w + \frac{\partial^2 w}{\partial z^2} \right]$$

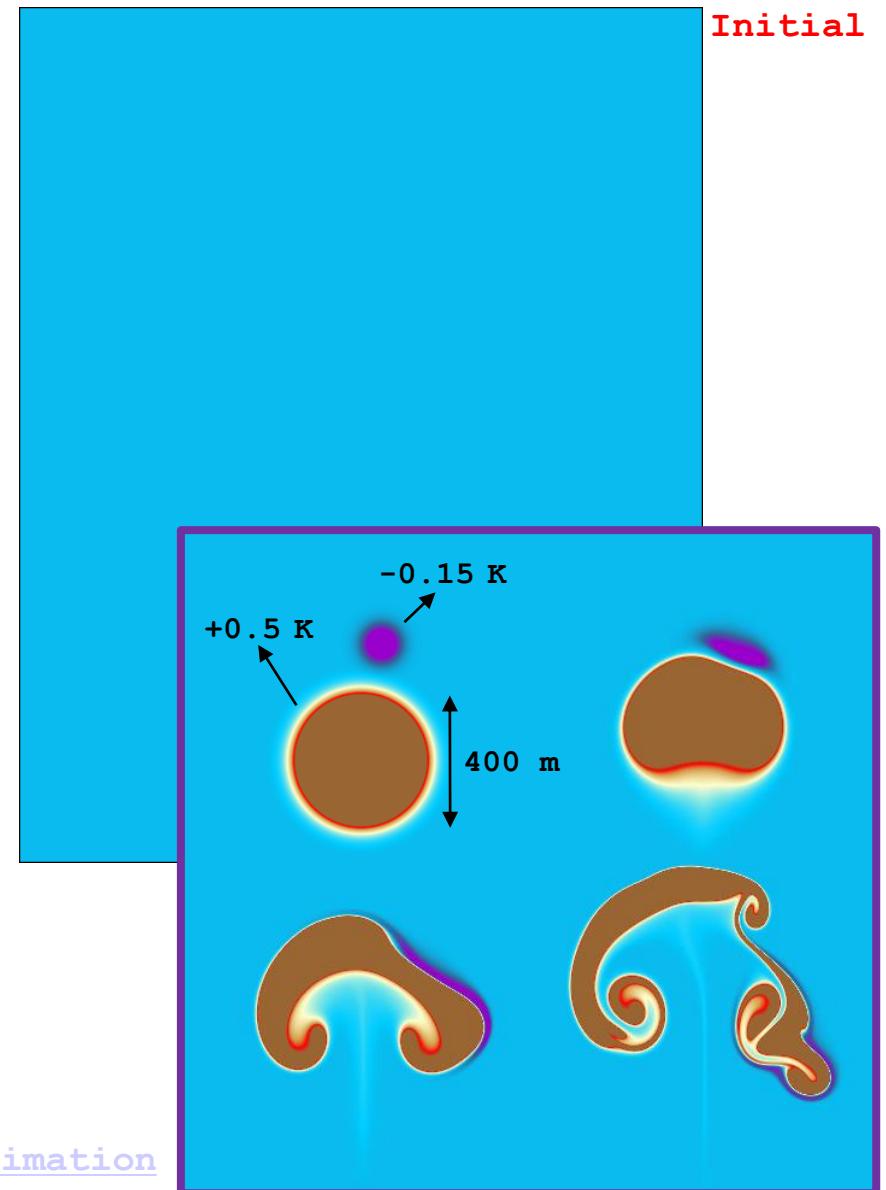
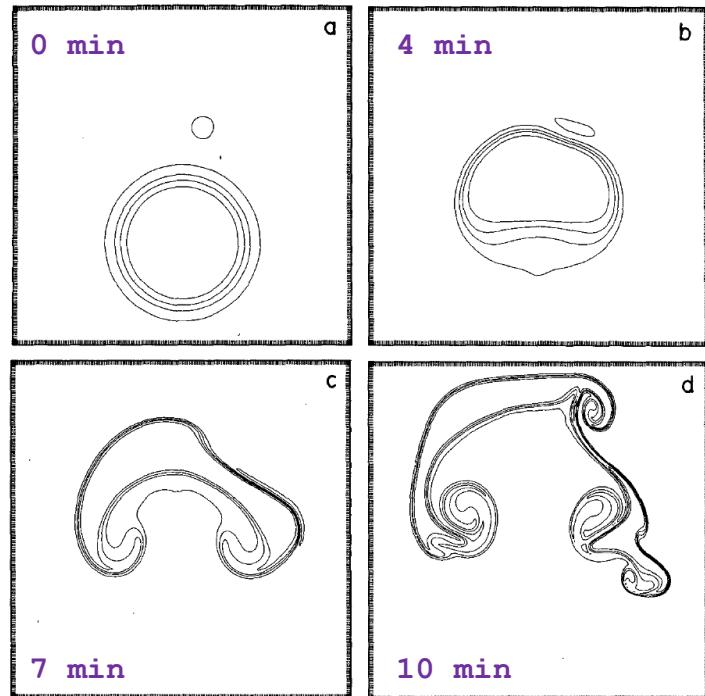
> Numerical implementation 3D [CFL $\xrightarrow{c_s > 300 \text{ m/s}}$ $\Delta t \approx 2 \Delta x (\Delta z)$]

- * Forward-Backward integration of "forcings" in RK2 cycle
- * REA (V and H) integration of advection every 6-10 Nsteps
- * Rigid Wall BCs at W/E S/N B/T boundaries

> Large Warm & Small Cold Bubbles

(dx=dz=2.5m, dt=0.00625s, Nstep=10, 40min)

Robert (1993)

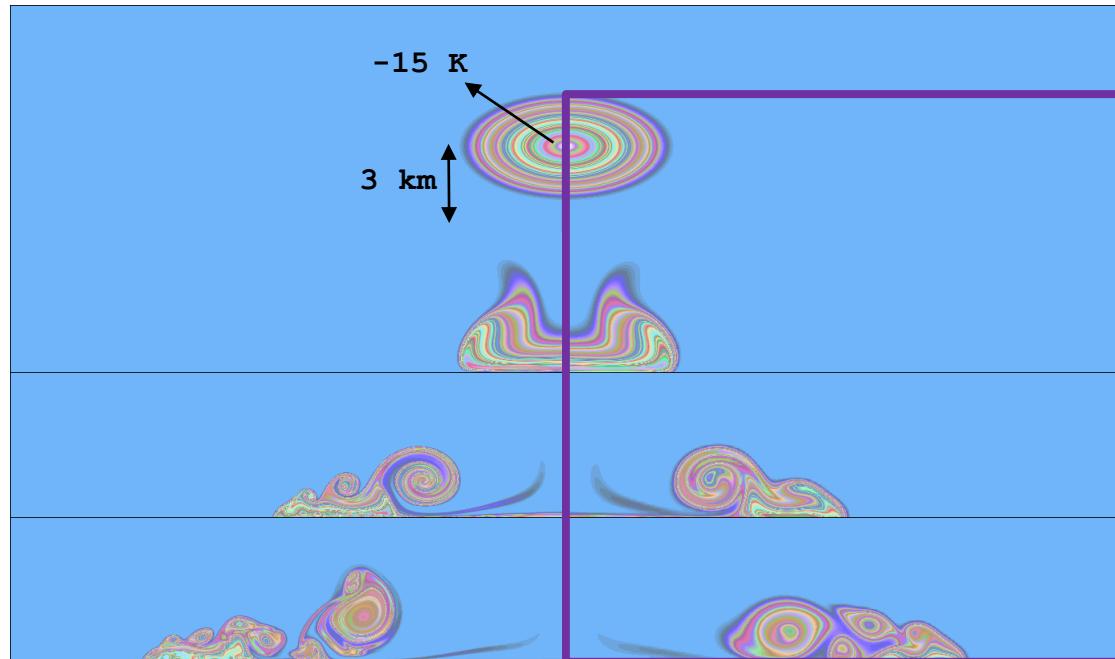


> Density Current

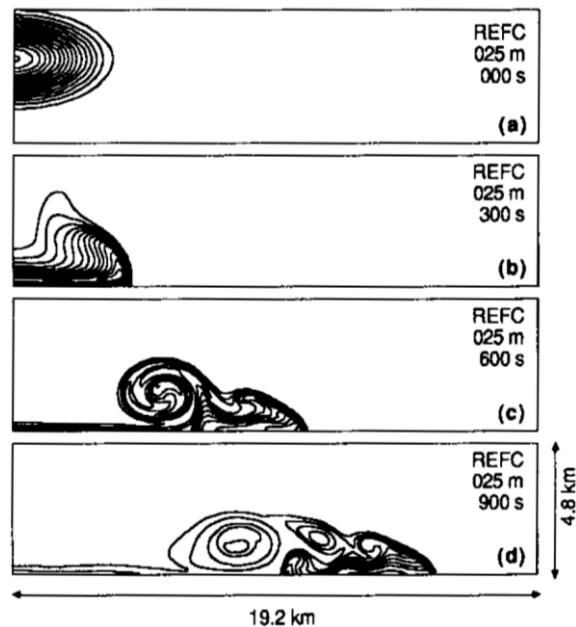
(dx=dz=100m, dt=0.25s, Nstep=10, 3h)

Quadruple resolution

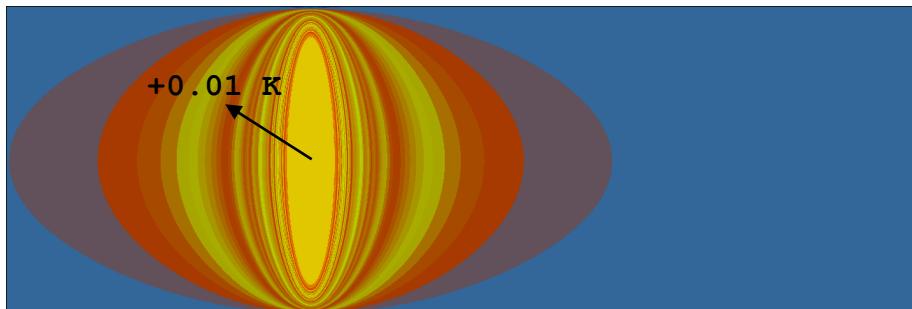
Initial



Straka et al. (1993)

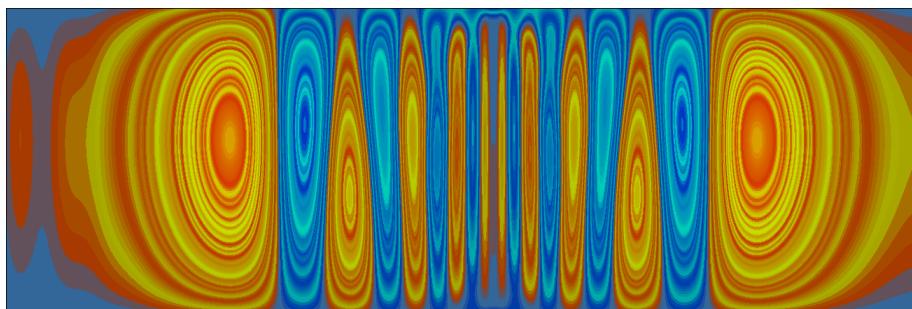
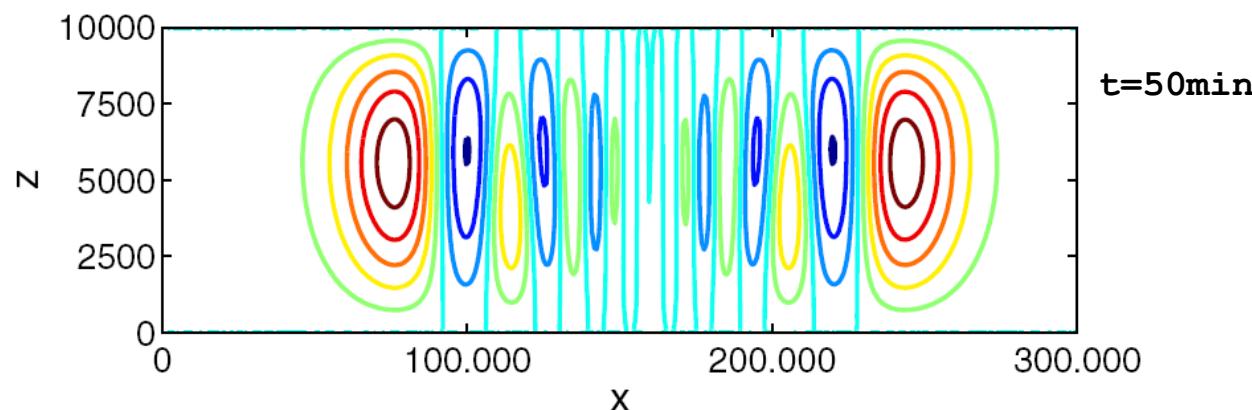


> Inertia-Gravity Waves (uniform wind/stability: $U=20\text{ms}^{-1}/N=0.01\text{s}^{-1}$)
($\Delta x = \Delta z = 125\text{m}$, $\Delta t = 0.3125\text{s}$, Nstep=10, **1h**)



Initial

Giraldo
&
Restelli
(2008)



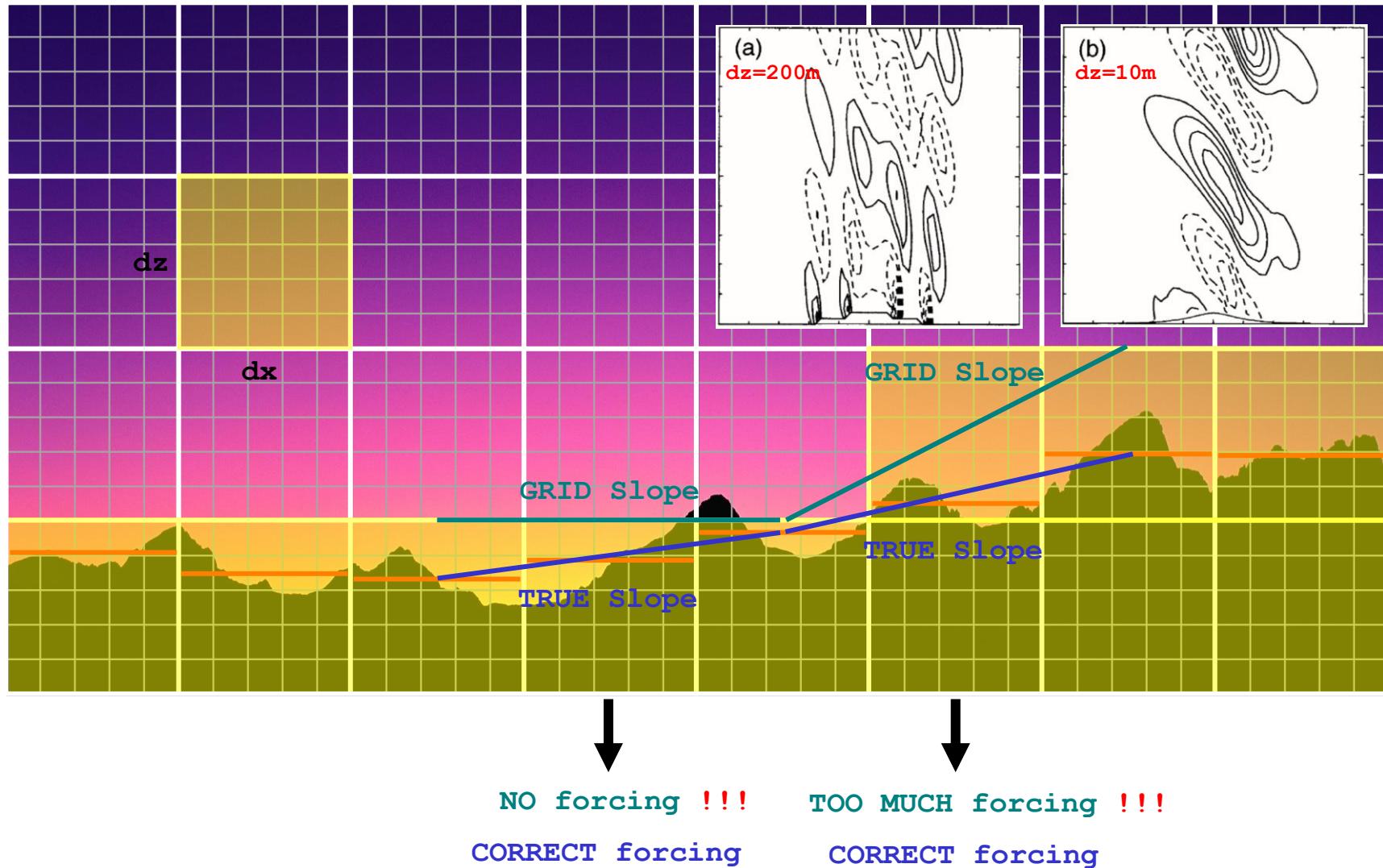
Animation

Inclusion of Orography (+ GW Absorbing Layer)

> TRUE-terrain slope **vs** GRID-based slope

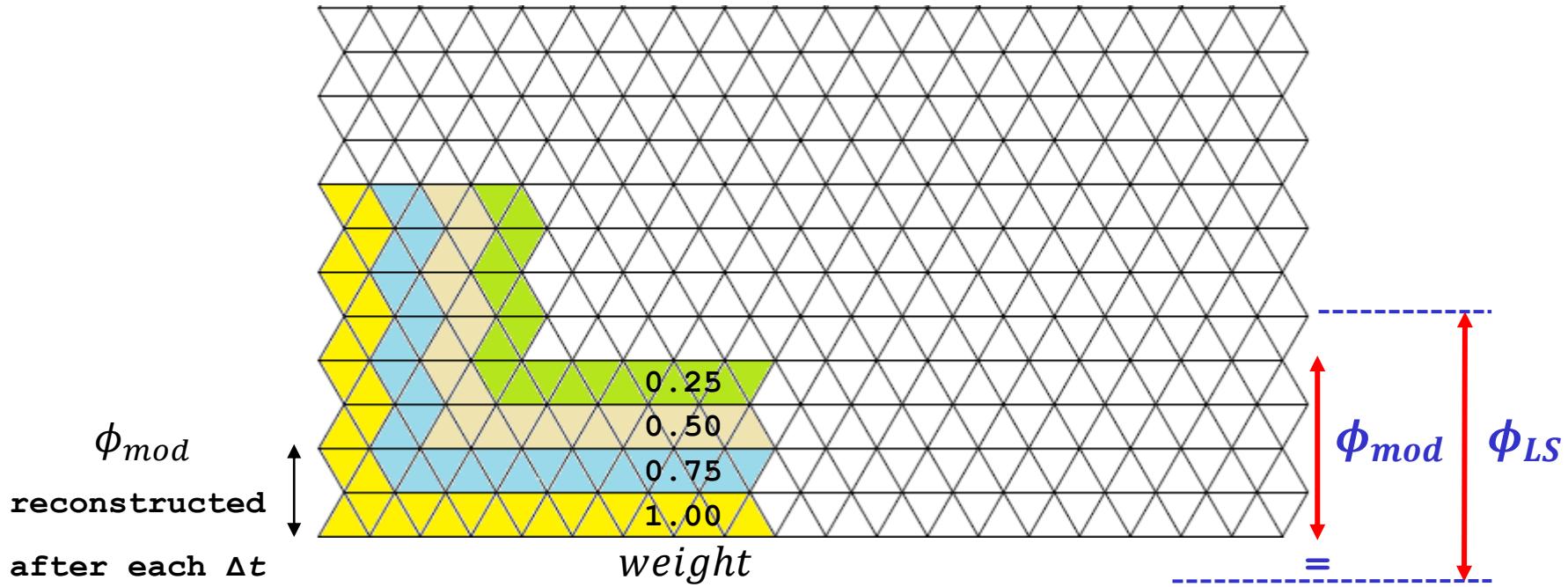
ETA MODEL

Gallus & Klemp (2000)



Specified Lateral Boundary Conditions

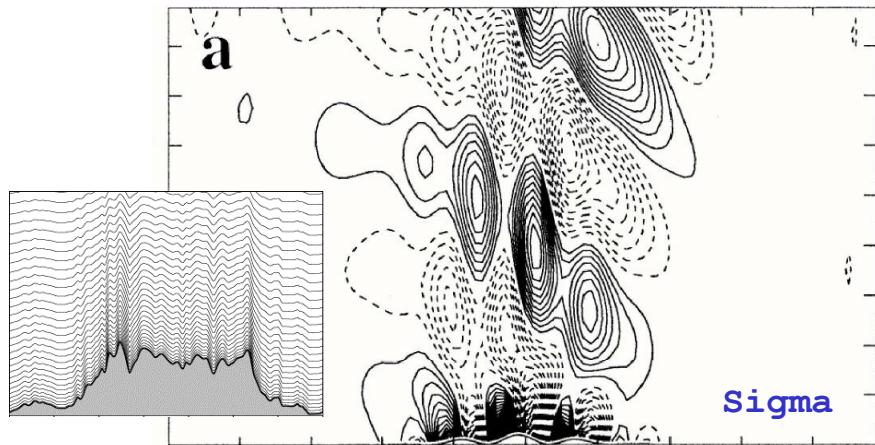
- > Interior solution ϕ_{mod} relaxed towards specified ϕ_{LS}



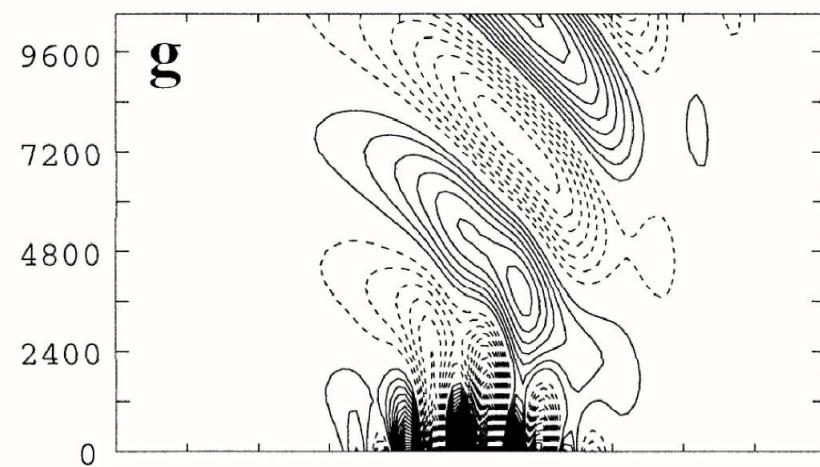
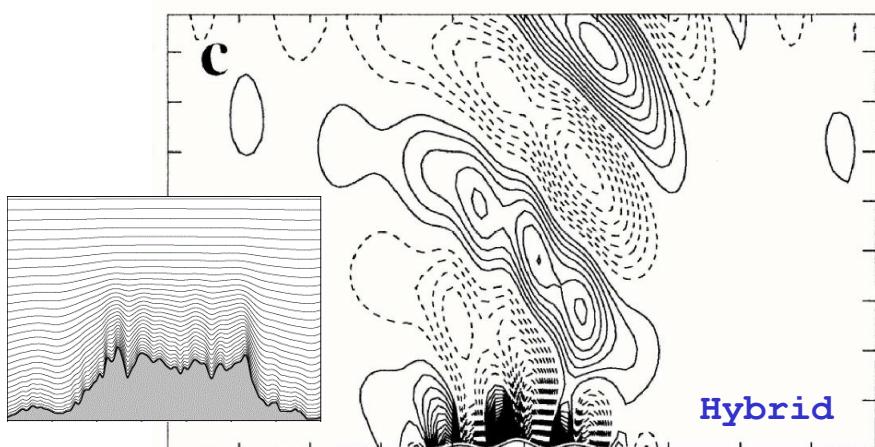
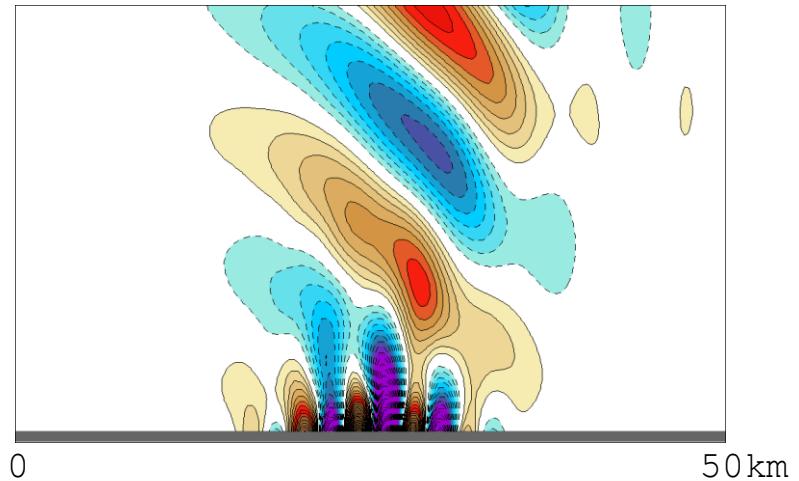
$$\frac{\partial \phi_{mod}}{\partial t} = weight [F(\phi_{LS} - \phi_{mod}) - G\Delta^2(\phi_{LS} - \phi_{mod})]$$

- > Typical values $\begin{cases} F = 1/10\Delta t \\ G = 1/50\Delta t \end{cases}$ ($\times 5$ if using grid analyses)

> Schär Mountain (250m bell-shaped + small-scale, $U=10\text{ms}^{-1}$, $N=0.01\text{s}^{-1}$)
($\Delta x=250\text{m}$, $\Delta z=250\text{m}$, $\Delta t=0.75\text{s}$, Nstep=10, 10h)



Steady-state

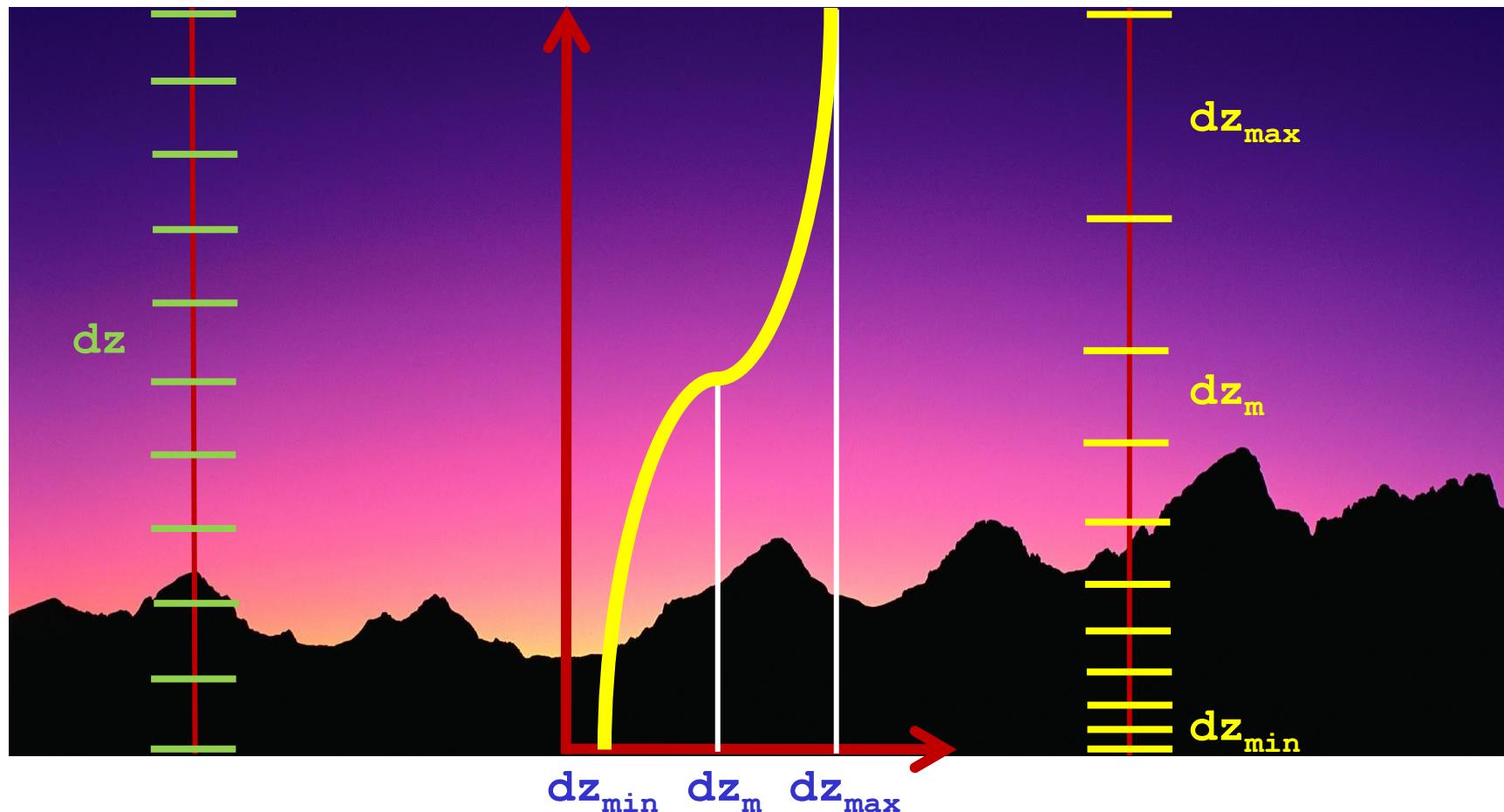


Schär et al. (2002)

Analytical

Vertical Stretching (+ Stabilization Fast Modes)

> Higher resolution at low levels (cos profile)



> Two parameters (stretch, dz_m)

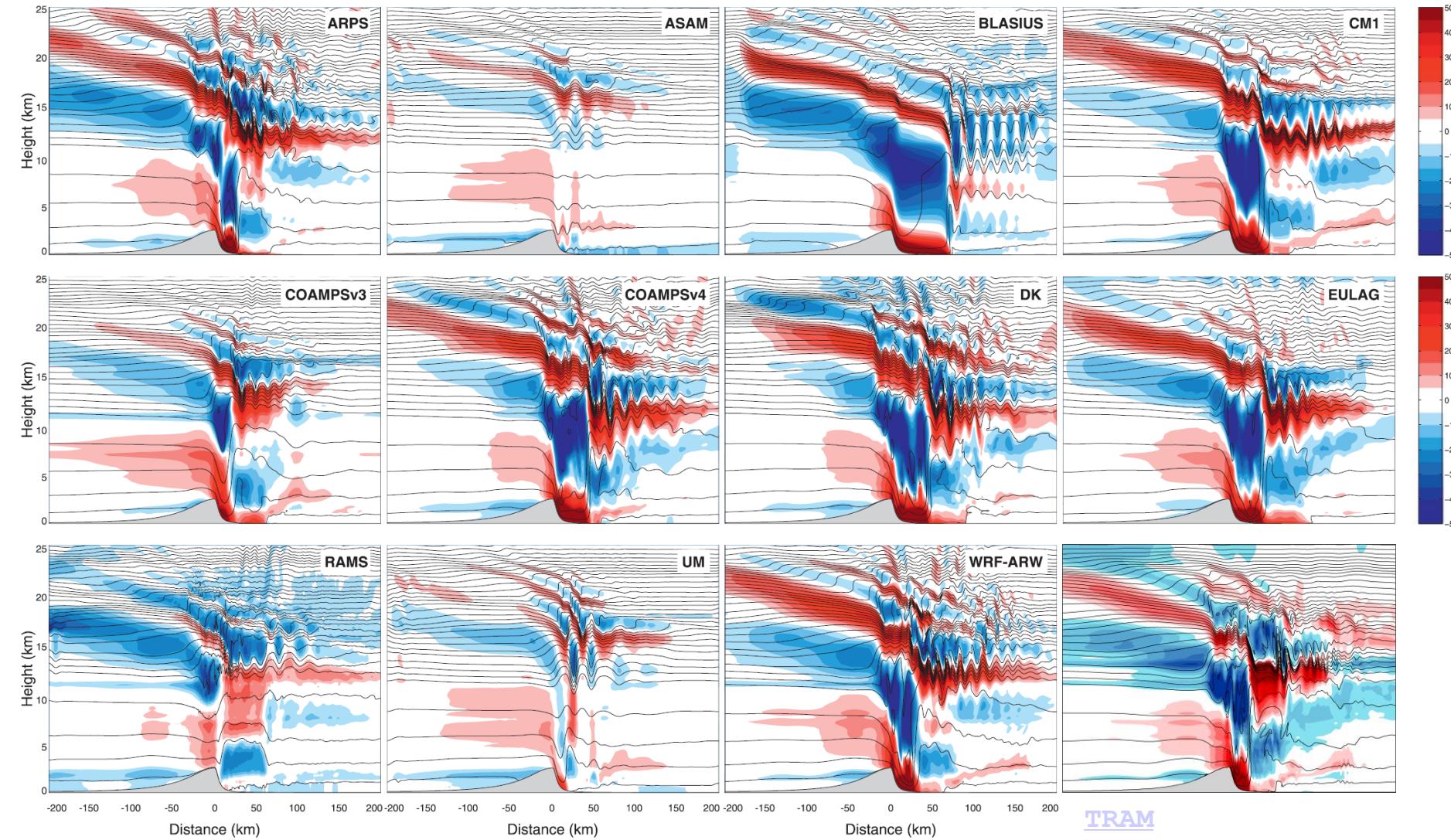
$$\begin{cases} dz_{min} = dz_m / \text{stretch} \\ dz_{max} = dz_m + (dz_m - dz_{min}) \end{cases}$$

> T-REX Intense Mountain-Wave

 $t=4\text{h}$

(dx=500m, dzm=100m, stretch=5, dt=1.5s, Nstep=6, 20h)

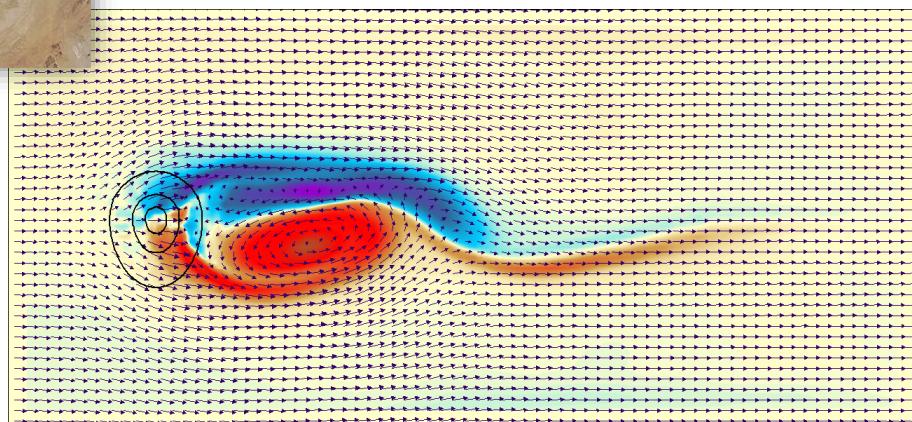
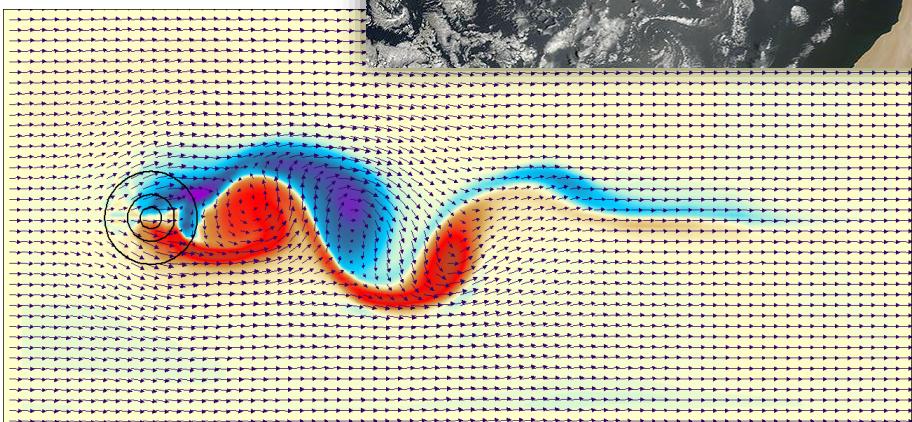
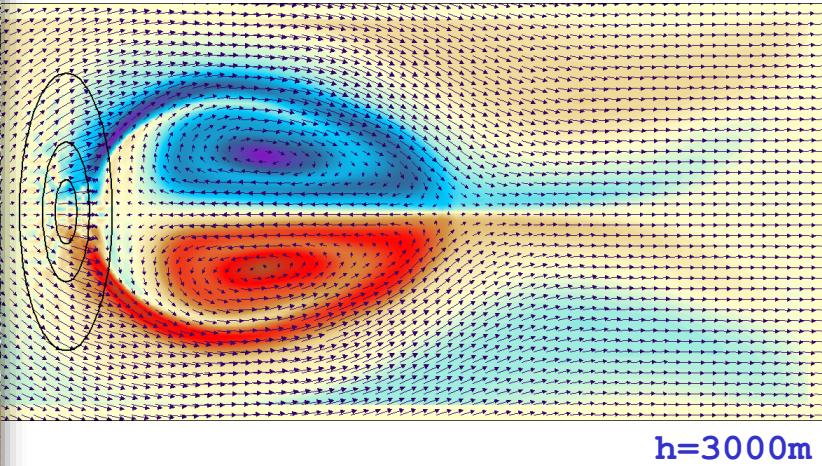
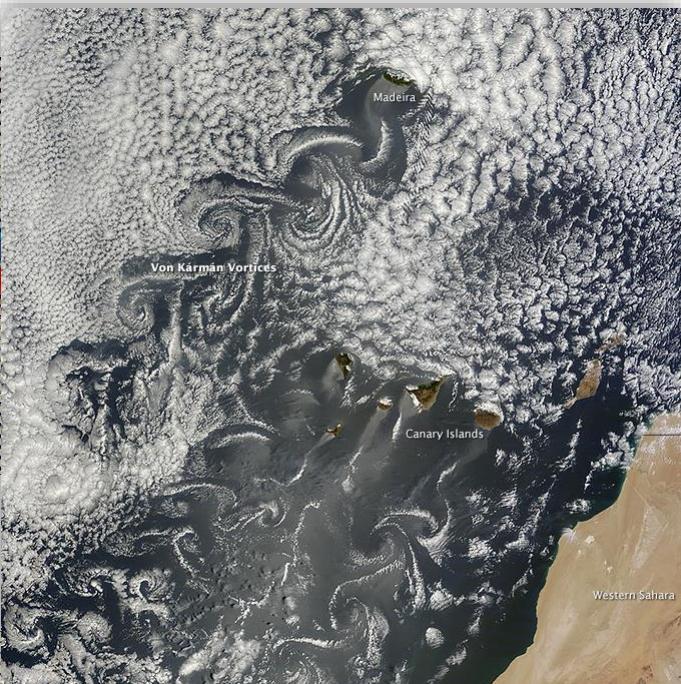
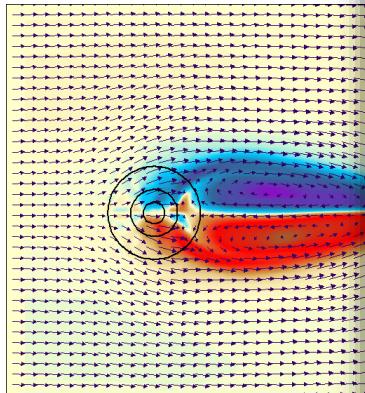
Doyle et al. (2011)


[TRAM](#)
[Anim](#)

> Von Kármán Vortex Streets ($U=10\text{ms}^{-1}$, $N=0.01\text{s}^{-1}$)

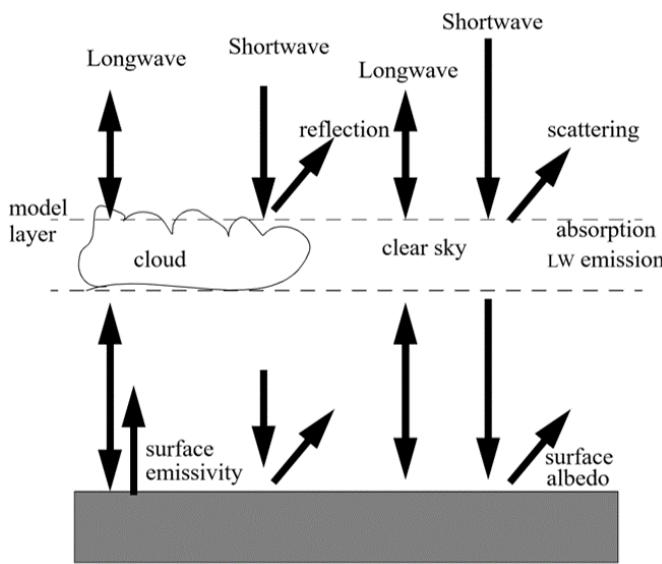
($\Delta x=2\text{km}$, $\Delta zm=500\text{m}$, stretch=2, $\Delta t=4\text{s}$, Nstep=10, 48h)

e.g. Schär and Durran (1997)

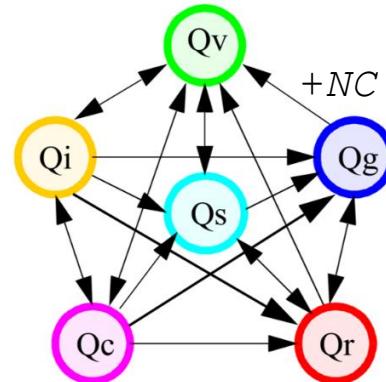


$h=3000\text{m}$

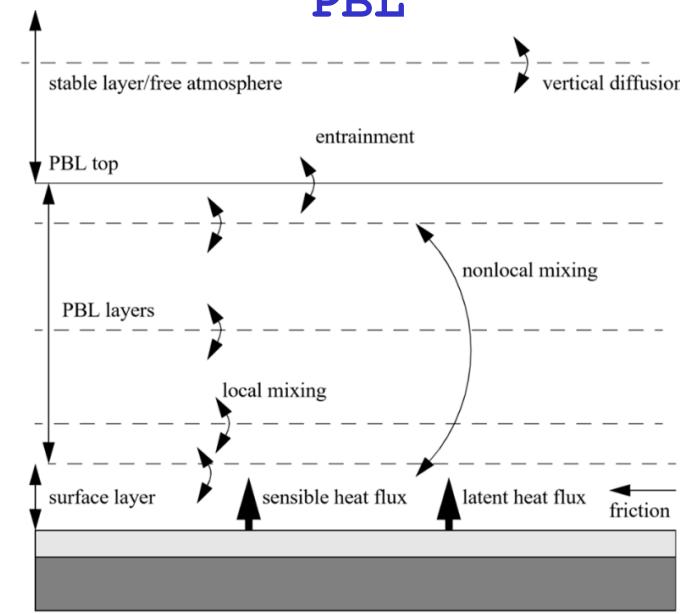
Radiation



Microphysics



PBL



NEW

Prognostic fields

$$Q_\chi$$

Forcing terms

$$F_{Q_\chi}$$

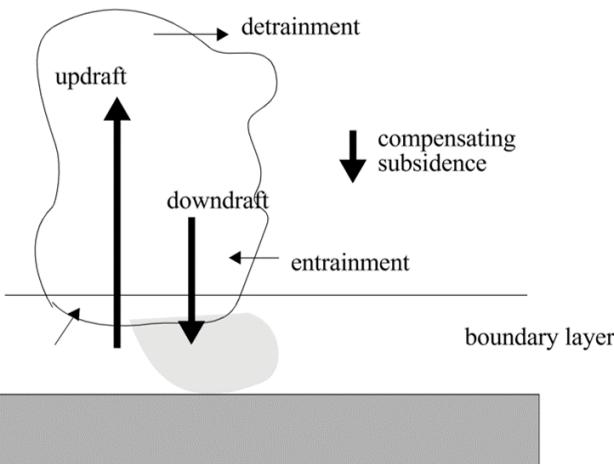
$$F_T$$

$$F_u \ F_v$$

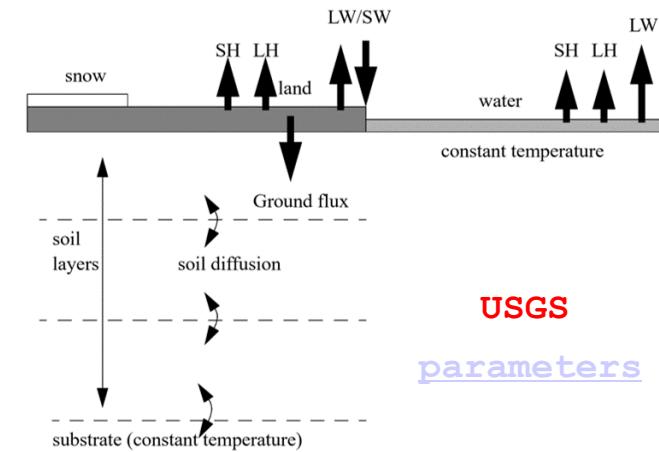
Surface variables

$$T_g \ R_{nc} \ R_c \ \dots$$

Cumulus



Surface



NEW Form of Equations: MESOSCALE-IDEALized

$$\frac{\partial \pi'}{\partial t} = -u \frac{\partial \pi'}{\partial x} - v \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right] + \frac{R_d}{c_{vm}} \frac{1}{\bar{\theta} + \theta'} F_T$$

**ALL moist effects
on pressure and
thermodynamics**

$$\frac{\partial \theta'}{\partial t} = -u \frac{\partial \theta'}{\partial x} - v \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} - \left(\frac{R_m}{c_{vm}} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} \right) (\bar{\theta} + \theta') \left[\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right]$$

**Physics computed
in NSTEP-cycle**

$$+ \frac{c_v}{c_{vm}} \frac{1}{\bar{\pi} + \pi'} F_T + \frac{R_v}{c_{vm}} \left(1 - \frac{R_d}{c_p} \frac{c_{pm}}{R_m} \right) (\bar{\theta} + \theta') F_{Q_v}$$

$$\frac{\partial u}{\partial t} = -u \frac{\partial u}{\partial x} - v \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial x} + f v - \hat{f} w + F_u$$

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial x} - v \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial y} - f u + F_v$$

$$\frac{\partial w}{\partial t} = -u \frac{\partial w}{\partial x} - v \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial z} + g \frac{\theta'_\rho}{\bar{\theta}_\rho} + \hat{f} u - g(Q_{liq} + Q_{ice})$$

$$\frac{\partial Q_\chi}{\partial t} = -u \frac{\partial Q_\chi}{\partial x} - v \frac{\partial Q_\chi}{\partial y} - w \frac{\partial Q_\chi}{\partial z} + F_{Q_\chi}$$

$\pi = \left(\frac{P}{P_0} \right)^{R_d/c_p} \quad \theta = \frac{T}{\pi} \quad P = \rho R_d T \frac{1+Q_v/\varepsilon}{1+Q_v}$
$\theta_\rho = \theta \frac{1+Q_v/\varepsilon}{1+Q_v+Q_{liq}+Q_{ice}} \quad c_p \bar{\theta}_\rho \frac{\partial \bar{\pi}}{\partial z} = -g$

$R_m = R_d + R_v \quad Q_v \quad \varepsilon = R_d / R_v$
$c_{pm} = c_p + c_{pv} \quad Q_v + c_l \quad Q_{liq} + c_i \quad Q_{ice}$
$c_{vm} = c_v + c_{vv} \quad Q_v + c_l \quad Q_{liq} + c_i \quad Q_{ice}$

NEW Form of Equations: SYNOPTIC-REALcase

$$\frac{\partial \pi'}{\partial t} = -mu \frac{\partial \pi'}{\partial x} - mv \frac{\partial \pi'}{\partial y} - w \frac{\partial \pi'}{\partial z} - w \frac{\partial \bar{\pi}}{\partial z} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \left[m^2 \left(\frac{\partial(\frac{u}{m})}{\partial x} + \frac{\partial(\frac{v}{m})}{\partial y} \right) + \frac{\partial w}{\partial z} \right] \\ + \frac{R_d}{c_{vm}} \frac{1}{\bar{\theta} + \theta'} \mathbf{F}_T + \frac{R_d}{c_p} \frac{R_v}{R_m} \frac{c_{pm}}{c_{vm}} (\bar{\pi} + \pi') \mathbf{F}_{Q_v}$$

ALL Coriolis and curvature terms

$$\frac{\partial \theta'}{\partial t} = -mu \frac{\partial \theta'}{\partial x} - mv \frac{\partial \theta'}{\partial y} - w \frac{\partial \theta'}{\partial z} - w \frac{\partial \bar{\theta}}{\partial z} - \left(\frac{R_m}{c_{vm}} - \frac{R_d}{c_p} \frac{c_{pm}}{c_{vm}} \right) (\bar{\theta} + \theta') \left[m^2 \left(\frac{\partial(\frac{u}{m})}{\partial x} + \frac{\partial(\frac{v}{m})}{\partial y} \right) + \frac{\partial w}{\partial z} \right] \\ + \frac{c_v}{c_{vm}} \frac{1}{\bar{\pi} + \pi'} \mathbf{F}_T + \frac{R_v}{c_{vm}} \left(1 - \frac{R_d}{c_p} \frac{c_{pm}}{R_m} \right) (\bar{\theta} + \theta') \mathbf{F}_{Q_v}$$

LAMBERT projection

$$\frac{\partial u}{\partial t} = -mu \frac{\partial u}{\partial x} - mv \frac{\partial u}{\partial y} - w \frac{\partial u}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) m \frac{\partial \pi'}{\partial x} + v \left(f + u \frac{\partial m}{\partial y} - v \frac{\partial m}{\partial x} \right) - \hat{f} w \cos \alpha \\ - \frac{uw}{a} + \mathbf{F}_u$$

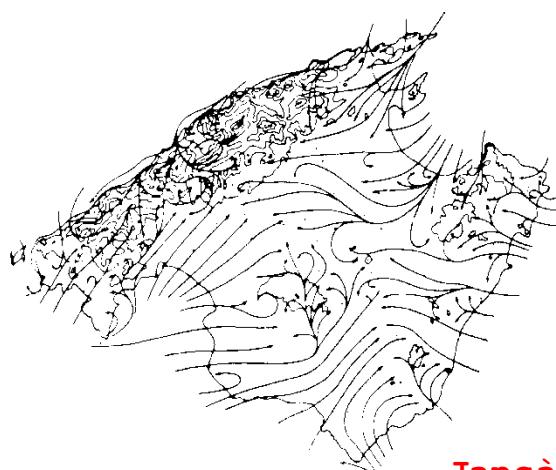
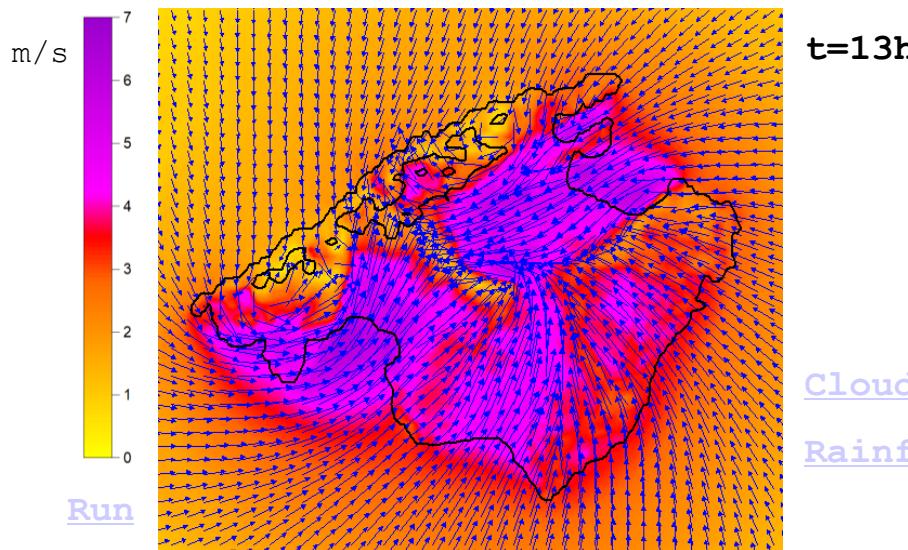
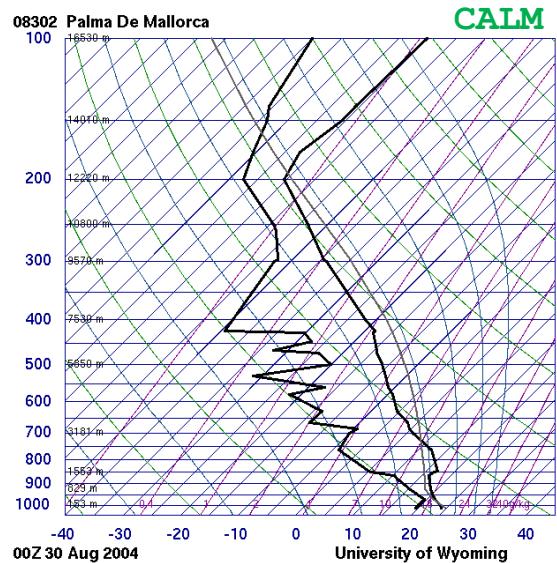
$$\frac{\partial v}{\partial t} = -mu \frac{\partial v}{\partial x} - mv \frac{\partial v}{\partial y} - w \frac{\partial v}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) m \frac{\partial \pi'}{\partial y} - u \left(f + u \frac{\partial m}{\partial y} - v \frac{\partial m}{\partial x} \right) + \hat{f} w \sin \alpha \\ - \frac{uw}{a} + \mathbf{F}_v$$

$$\frac{\partial w}{\partial t} = -mu \frac{\partial w}{\partial x} - mv \frac{\partial w}{\partial y} - w \frac{\partial w}{\partial z} - c_p (\bar{\theta}_\rho + \theta'_\rho) \frac{\partial \pi'}{\partial z} + g \frac{\theta'_\rho}{\bar{\theta}_\rho} + \hat{f} (u \cos \alpha - v \sin \alpha) \\ + \frac{u^2 + v^2}{a} - g (Q_{liq} + Q_{ice})$$

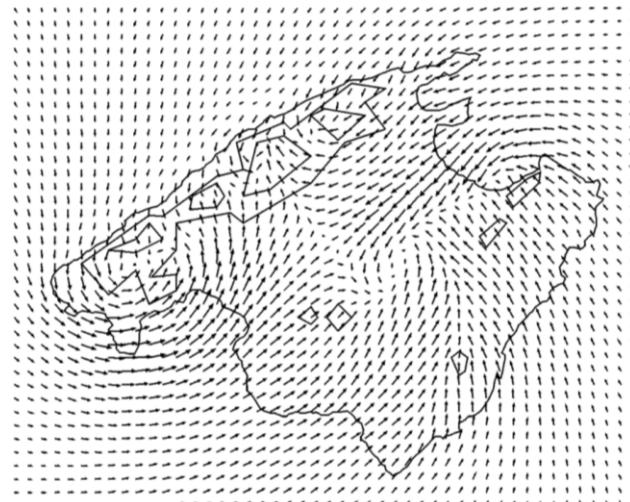
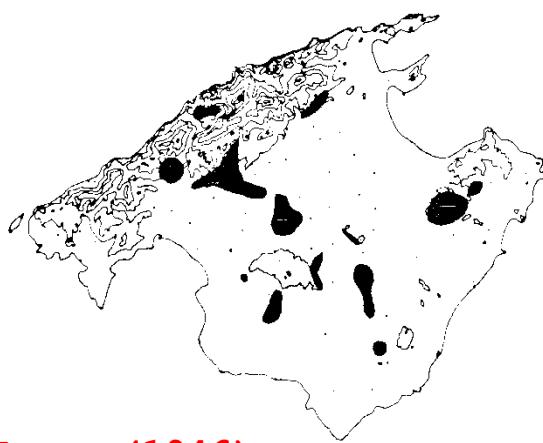
$$\frac{\partial Q_X}{\partial t} = -mu \frac{\partial Q_X}{\partial x} - mv \frac{\partial Q_X}{\partial y} - w \frac{\partial Q_X}{\partial z} + \mathbf{F}_{Q_X}$$

> Breeze Circulation in Mallorca (IC: Sounding 00 UTC 30 Ago 2004)

(dx=1.5km, dzm=400m, stretch=20, dt=3s, Nstep=10, 30h)



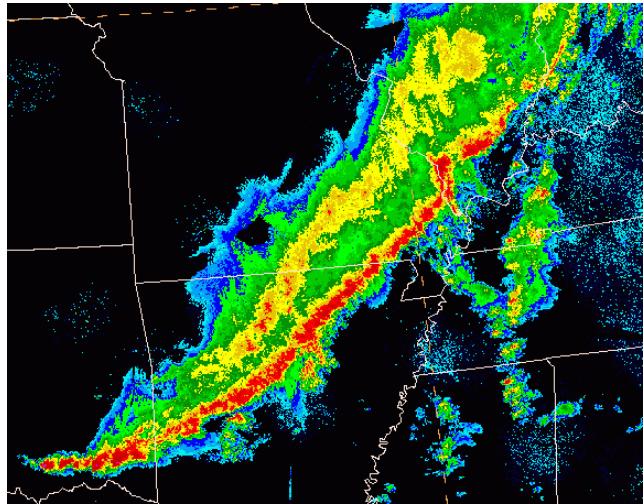
Jansà & Jaume (1946)



Ramis & Romero (1995)

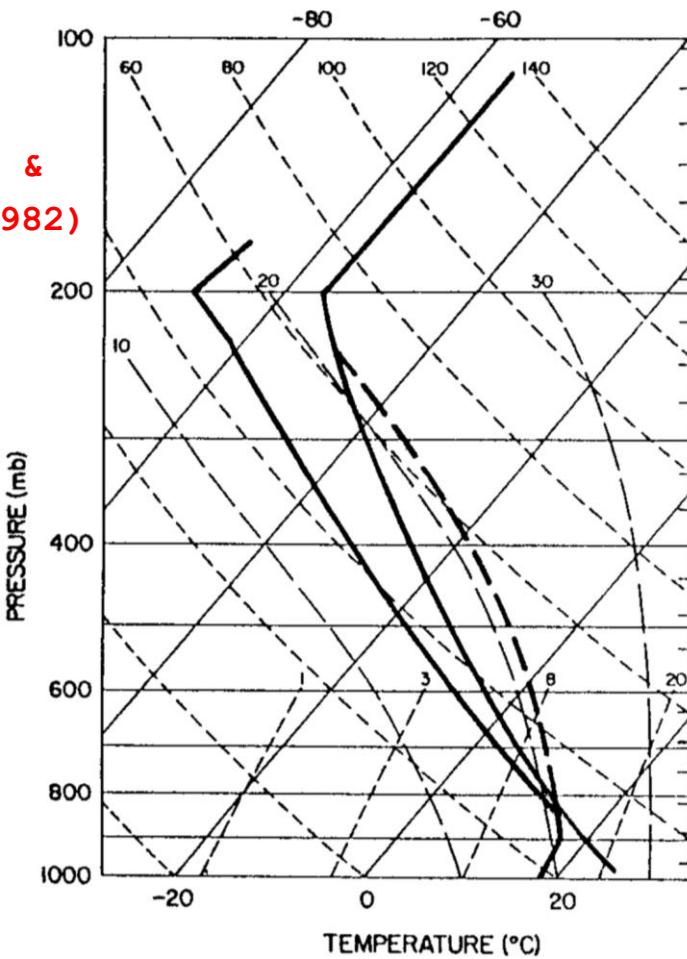
> Squall-Line Simulation (**NO** Coriolis, Radiation, PBL and Cumulus)

($\text{dx}=1.5\text{km}$, $\text{dzm}=200\text{m}$, $\text{stretch}=10$, $\text{dt}=3\text{s}$, $\text{Nstep}=5$, **10h**)



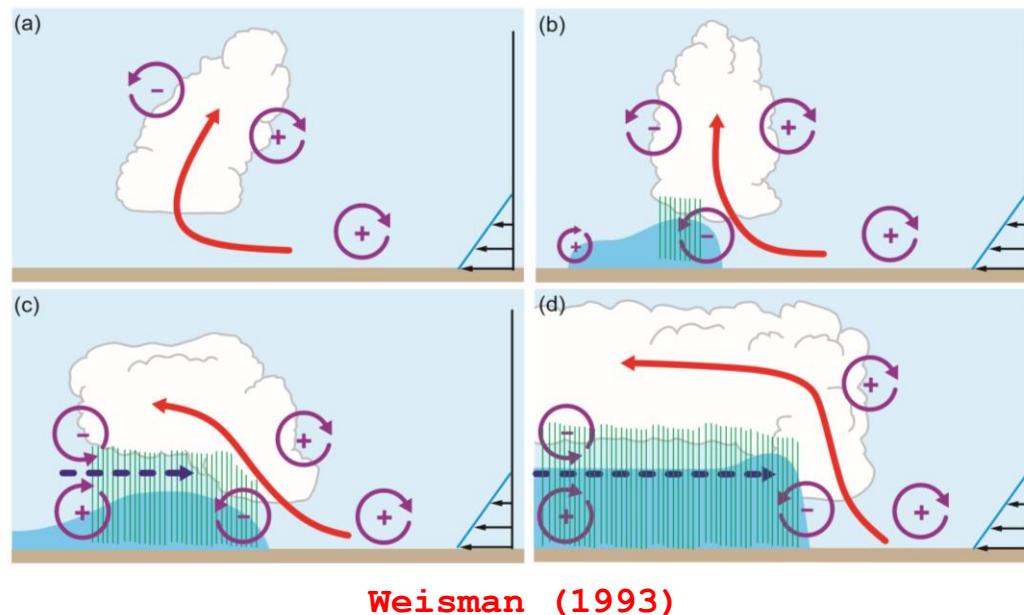
IC: WK82 SOUNDING + 8K Surface Cold Pool
... and 3 different wind profiles

Weisman &
Klemp (1982)

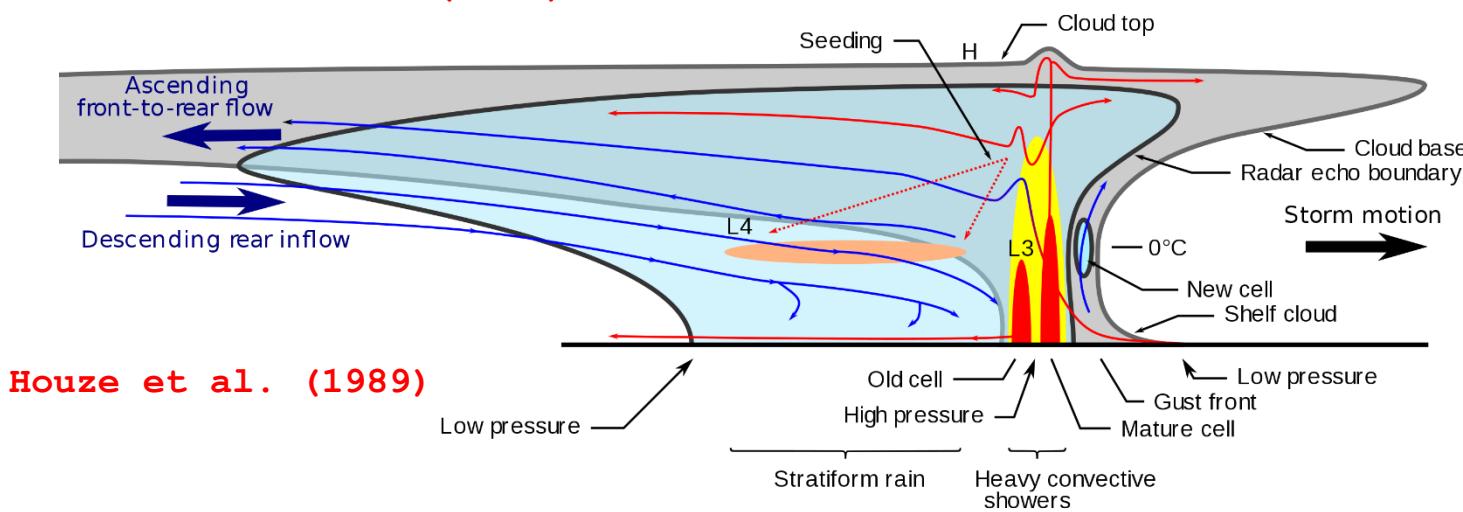
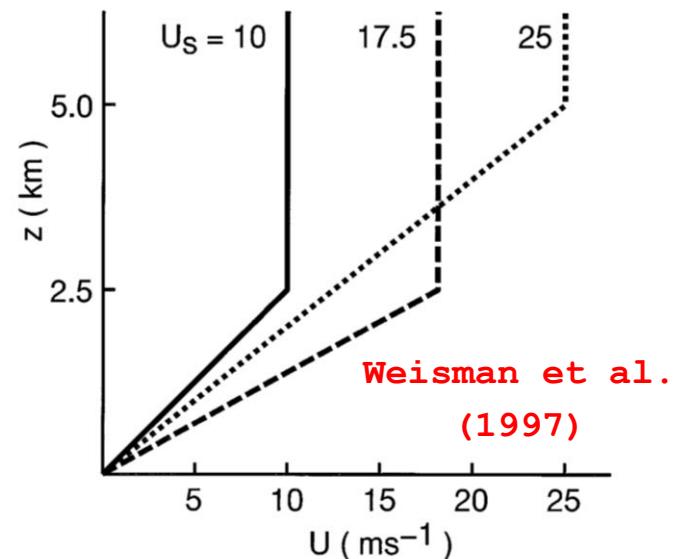


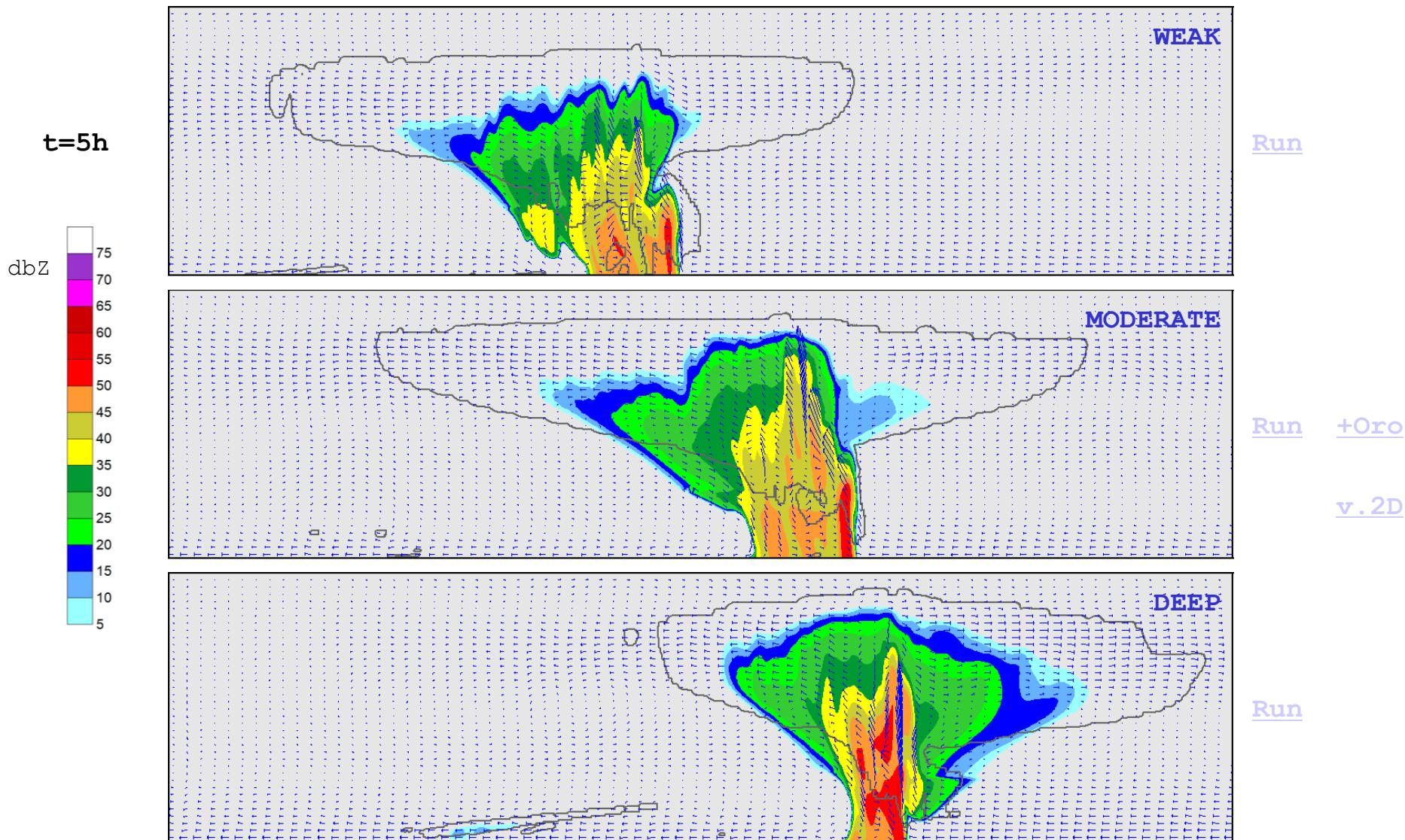
> Squall-Line Simulation (NO Coriolis, Radiation, PBL and Cumulus)

(dx=1.5km, dzm=200m, stretch=10, dt=3s, Nstep=5, 10h)

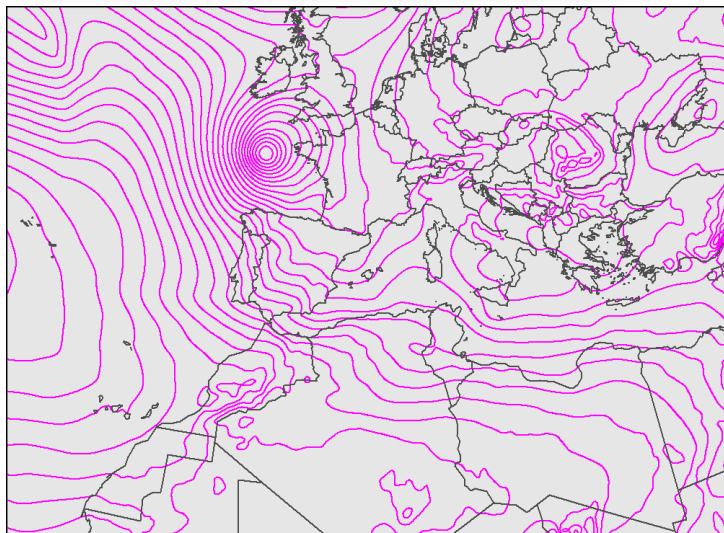
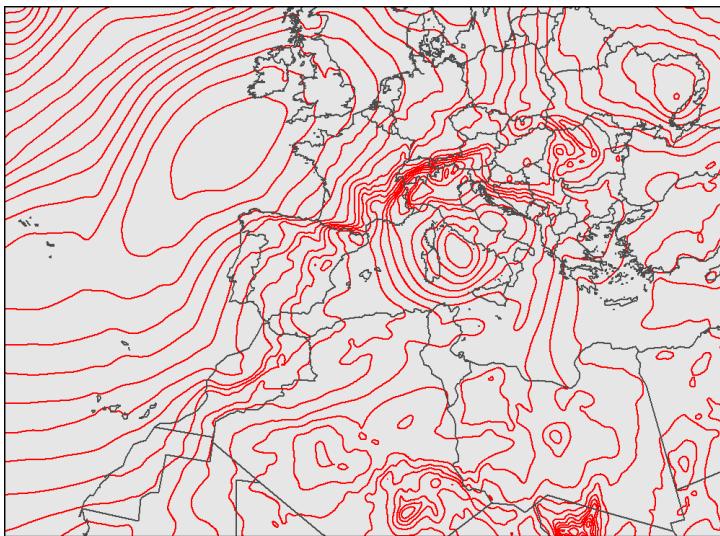
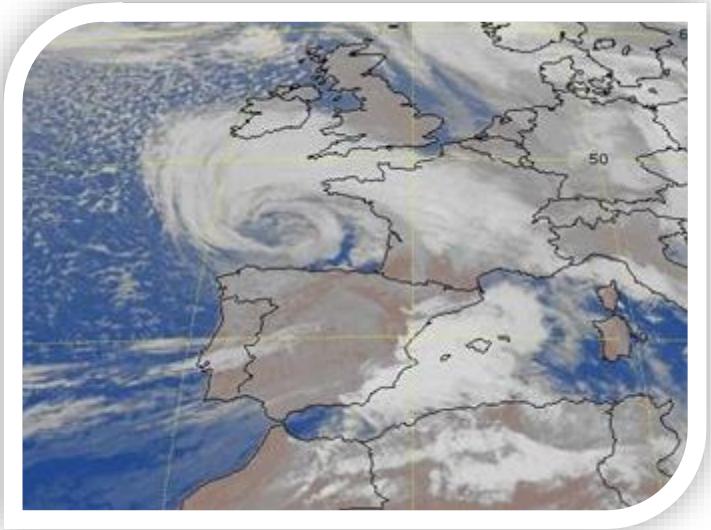
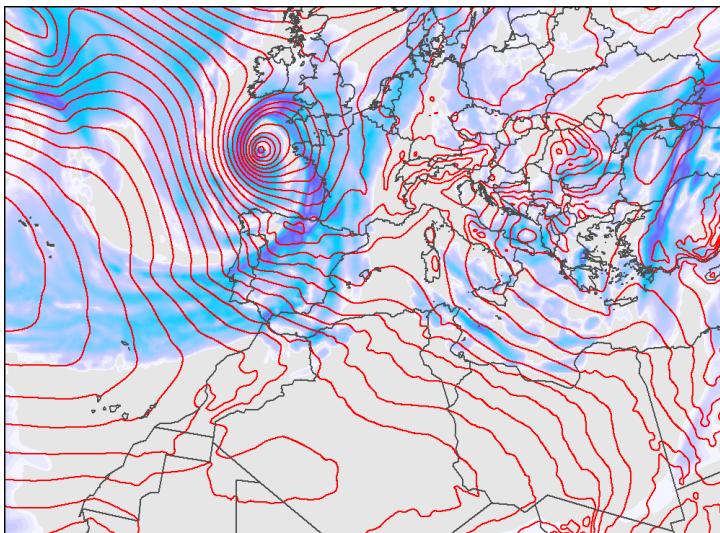


SHEAR: Weak Moderate Deep



> Squall-Line Simulation (**NO** Coriolis, Radiation, PBL and Cumulus)(dx=1.5km, dzm=200m, stretch=10, dt=3s, Nstep=5, **10h**)

> "HUGO" Intense Cyclonic Storm (IC: 00 UTC 21 Mar 2018)

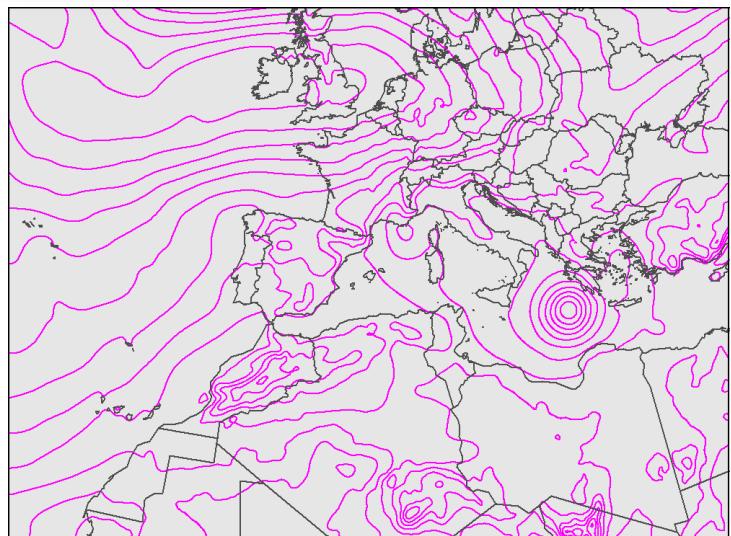
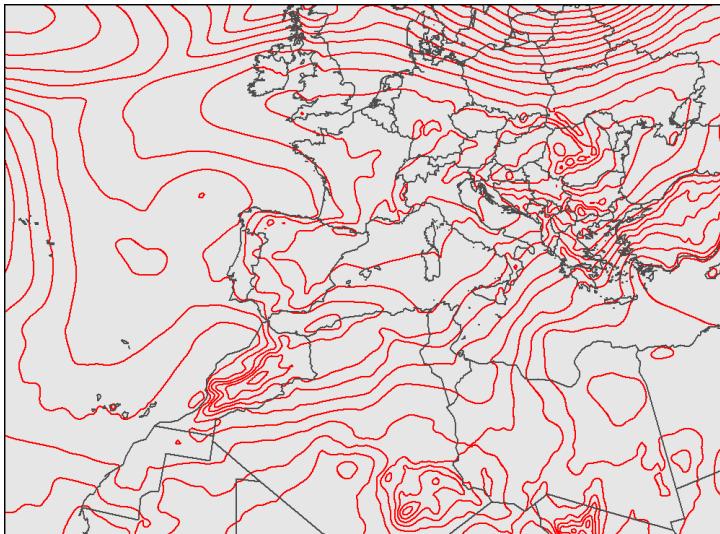
(MR: $dx=25\text{km}$, $dzm=200\text{m}$, $\text{stretch}=10$, $dt=45\text{s}$, $N_{\text{step}}=5$, 90h) $t=72\text{h}$ Windskg/m²

4
3.6
3.2
2.8
2.4
2.0
1.6
1.2
0.8
0.4
0

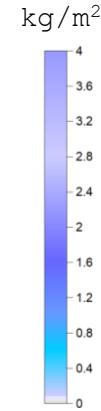
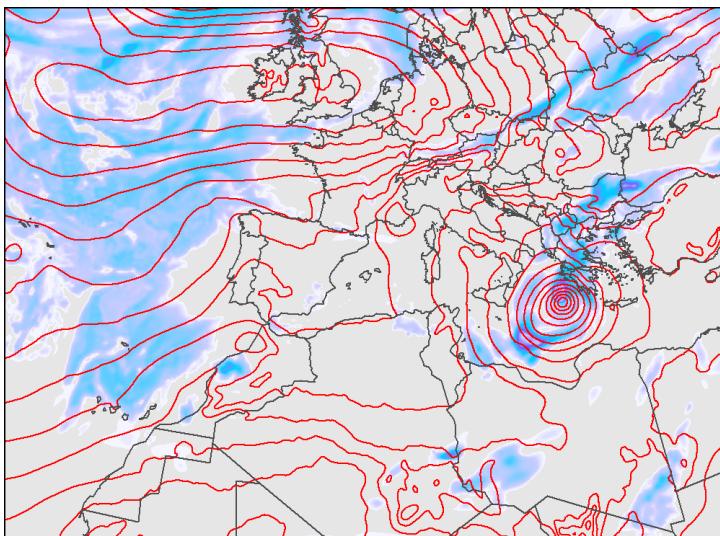
TRAM

Rainfall

> "ZORBAS" Ionian Sea Medicane (IC: 00 UTC 27 Sept 2018)

(MR: $dx=25\text{km}$, $dzm=200\text{m}$, $\text{stretch}=10$, $dt=45\text{s}$, $N_{\text{step}}=5$, 90h)

t=48h



TRAM

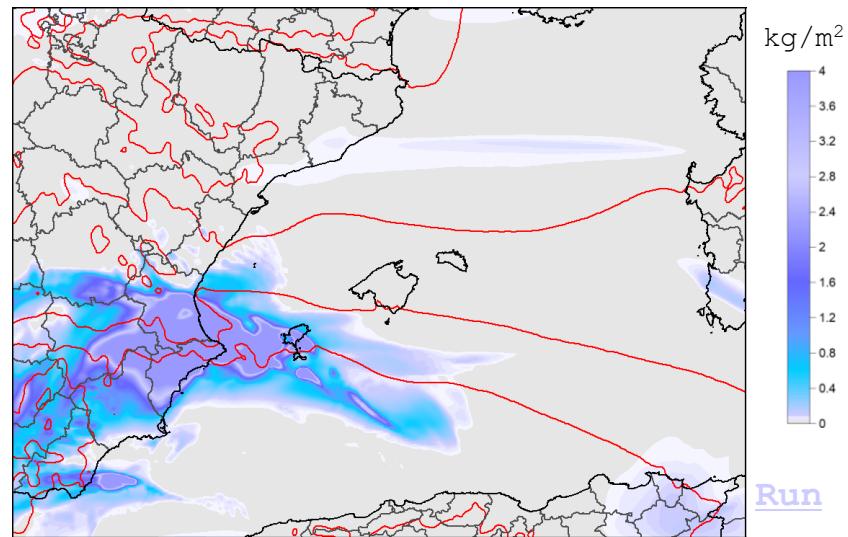
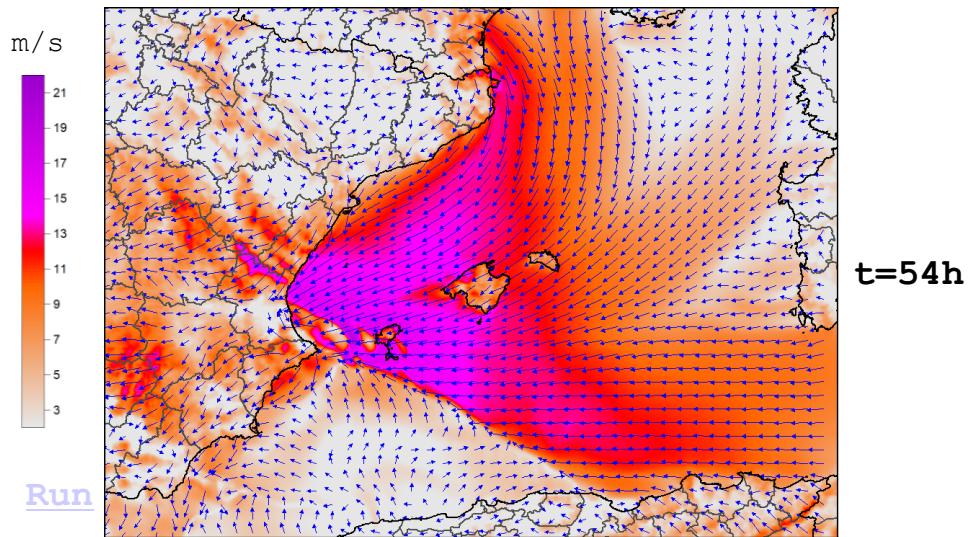
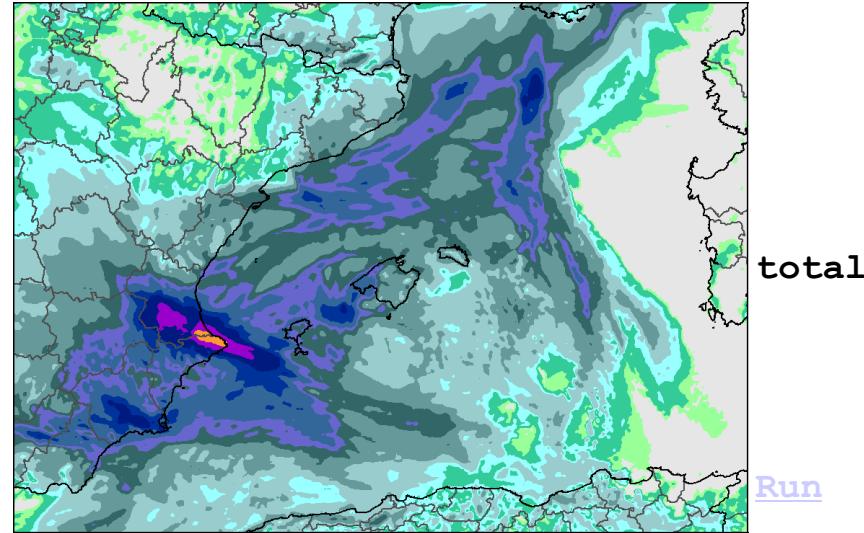
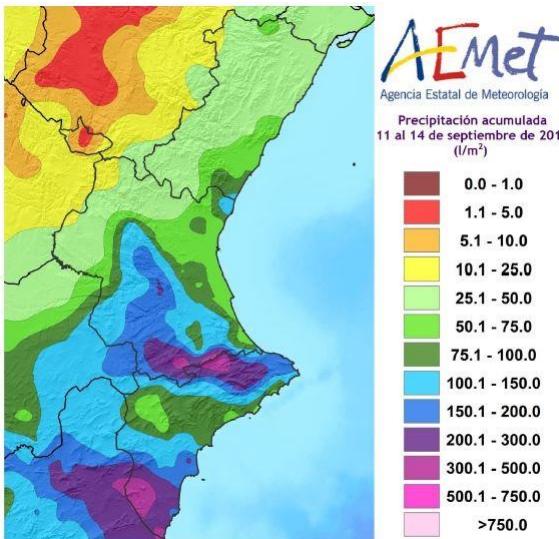
Winds

Rainfall

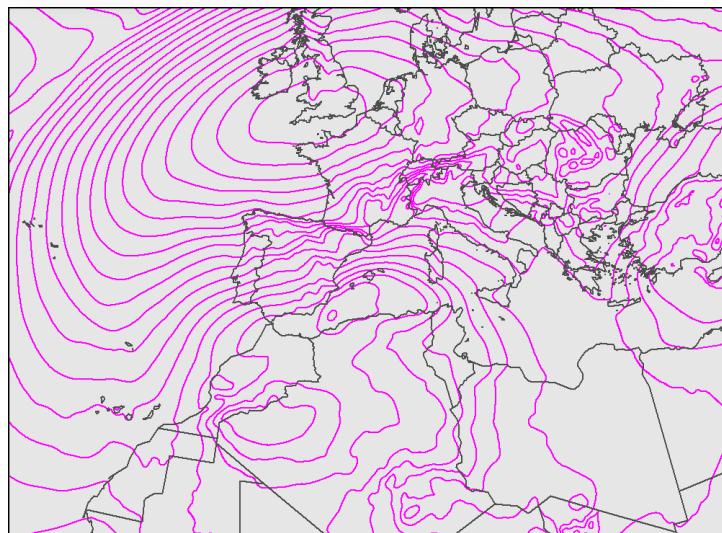
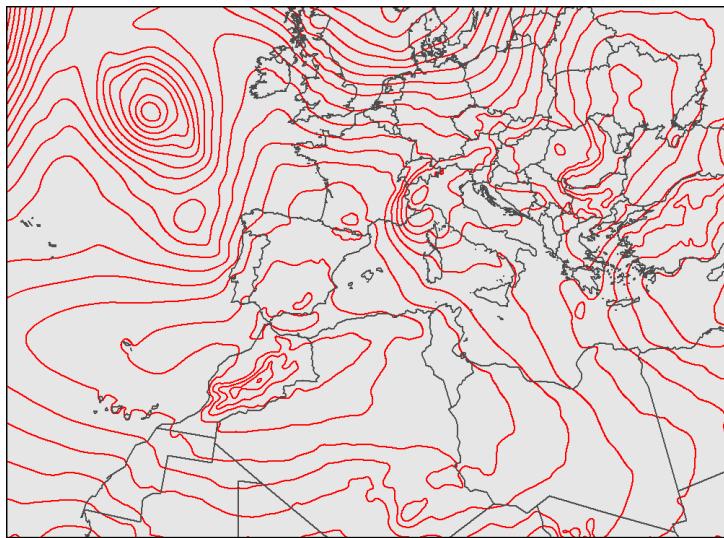
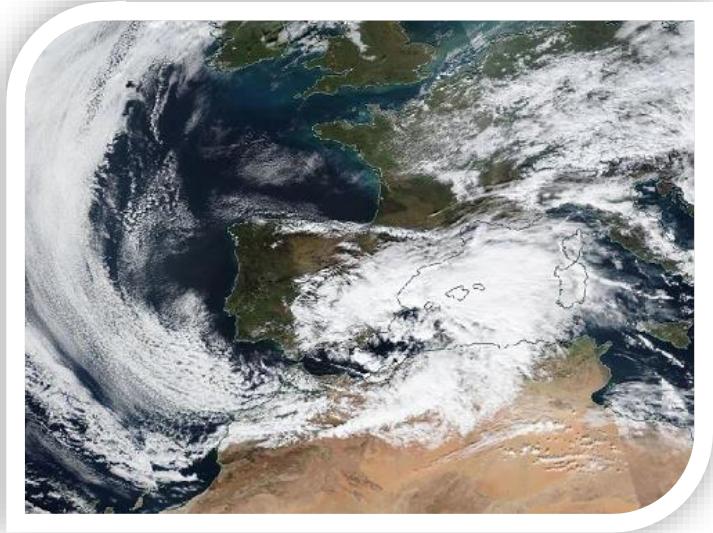
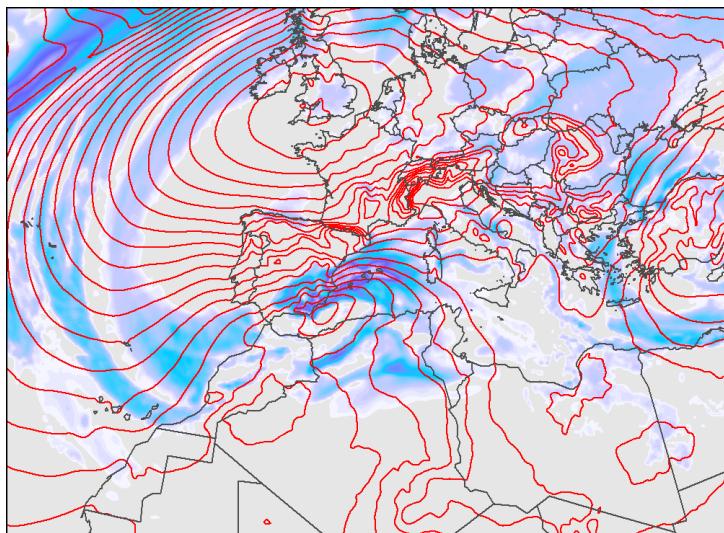
ERA-5

> "DANA" Valencia-Murcia Floods (IC: 00 UTC 10 Sept 2019)

(HR_double: dx=4.5km, dzm=200m, stretch=10, dt=9s, Nstep=5, 90h)



> "GLORIA" Extraordinary Storm (IC: 00 UTC 18 Jan 2020)

(MR: $dx=25\text{km}$, $dzm=200\text{m}$, $\text{stretch}=10$, $dt=45\text{s}$, $N_{\text{step}}=5$, 138h) $t=48\text{h}$ 

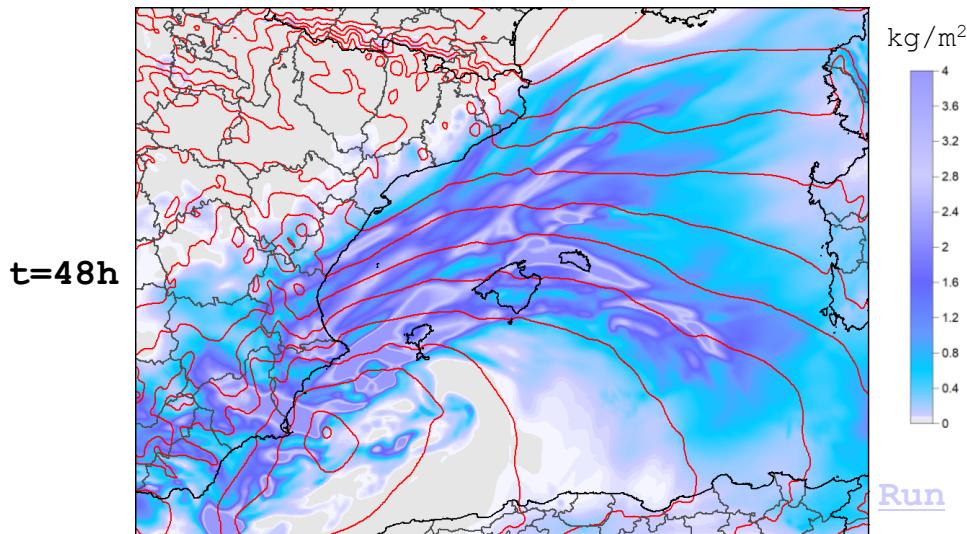
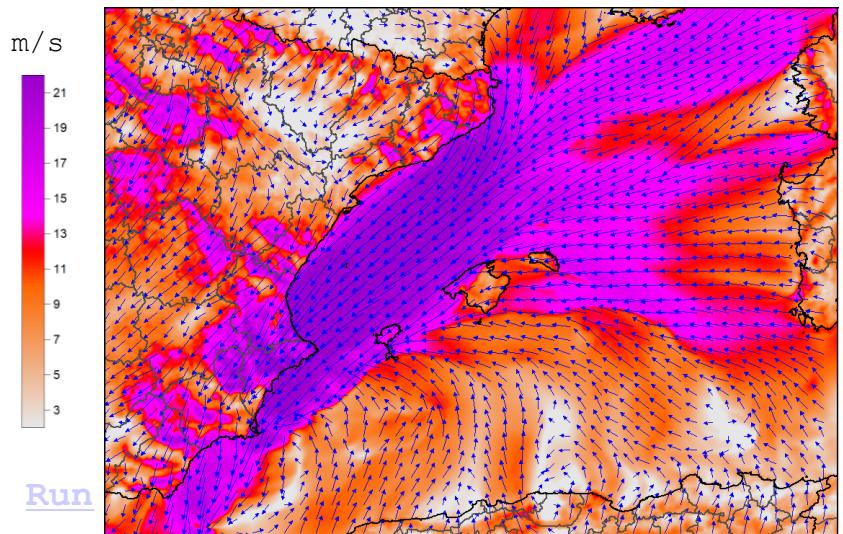
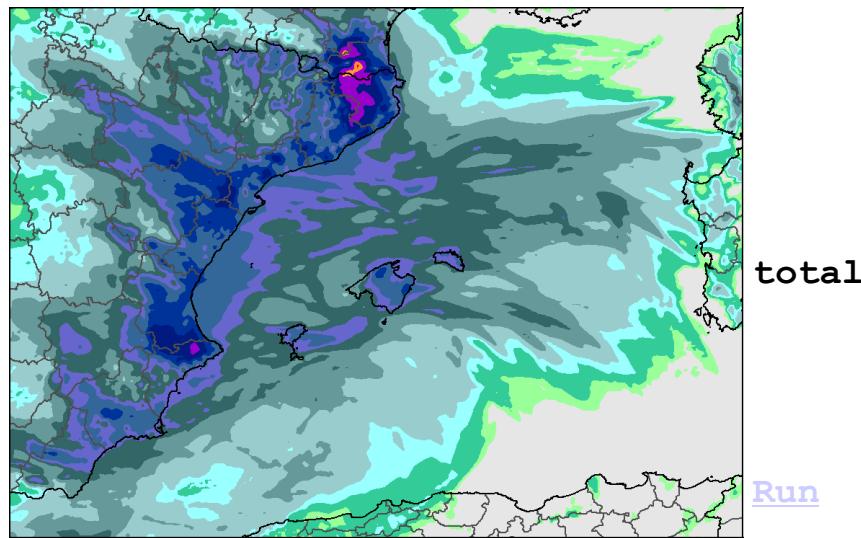
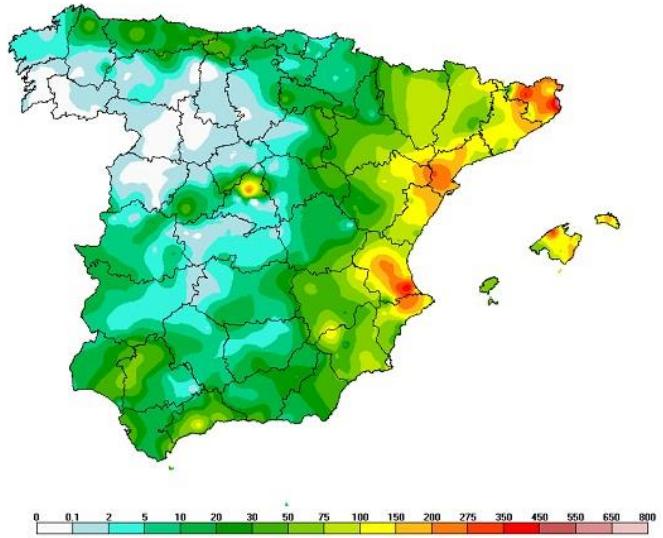
ERA-5

Winds

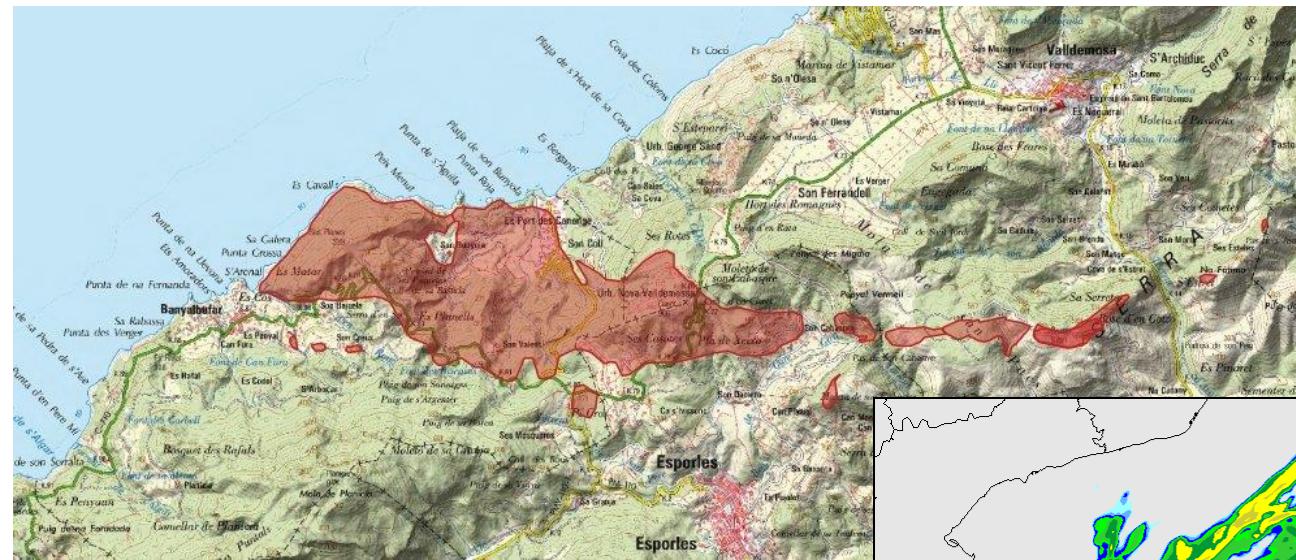
Rainfall

> "GLORIA" Extraordinary Storm (IC: 00 UTC 18 Jan 2020)

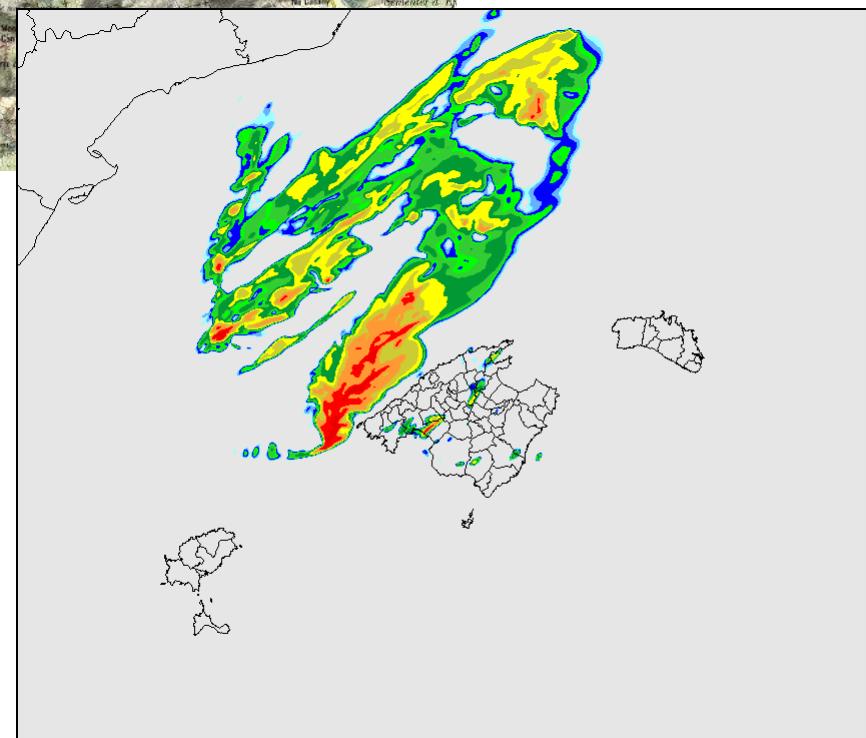
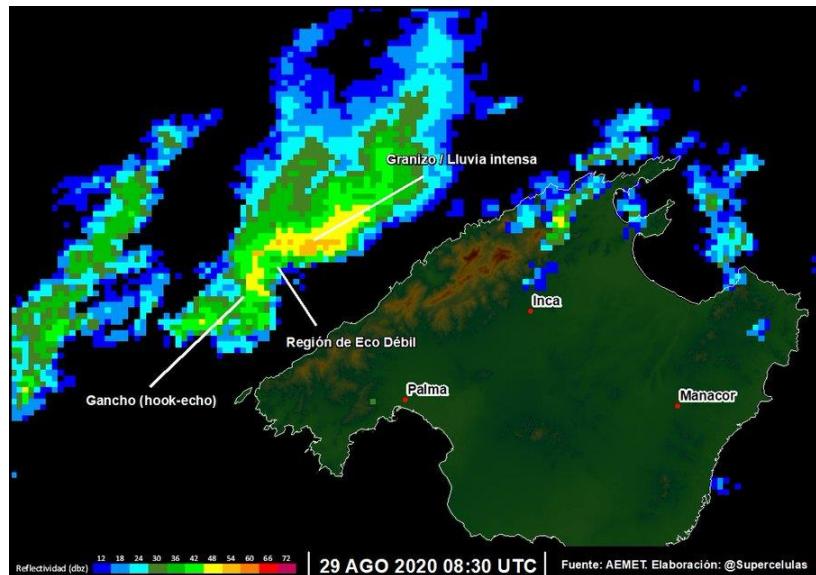
(HR_double: dx=4.5km, dzm=200m, stretch=10, dt=9s, Nstep=6, 138h)



> 29/00-29/18 TRAM Simulation ($\text{dx}=0.75\text{km}$, [GFS-fcst](#))



[Run](#)



Wind

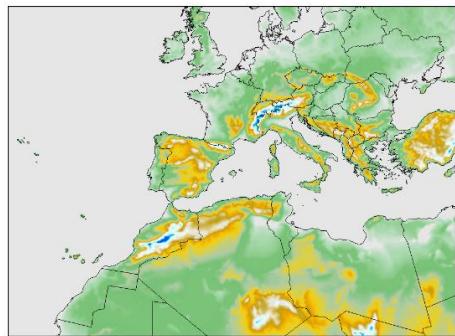
Speed

Rainfall

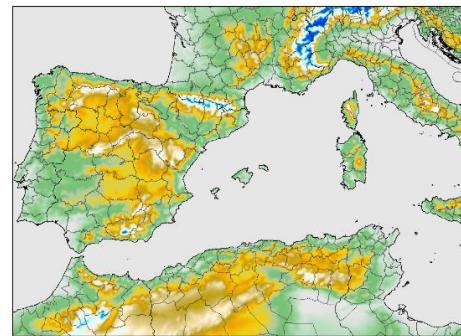
Temperature

TRAM / MeteoUIB

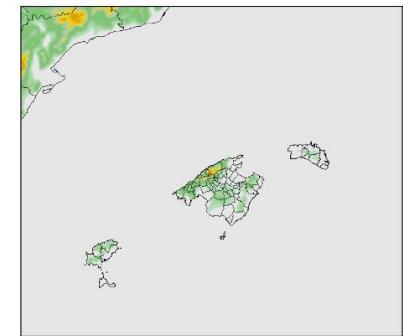
MR (17 km)



HR (6 km)



SR (2 km)



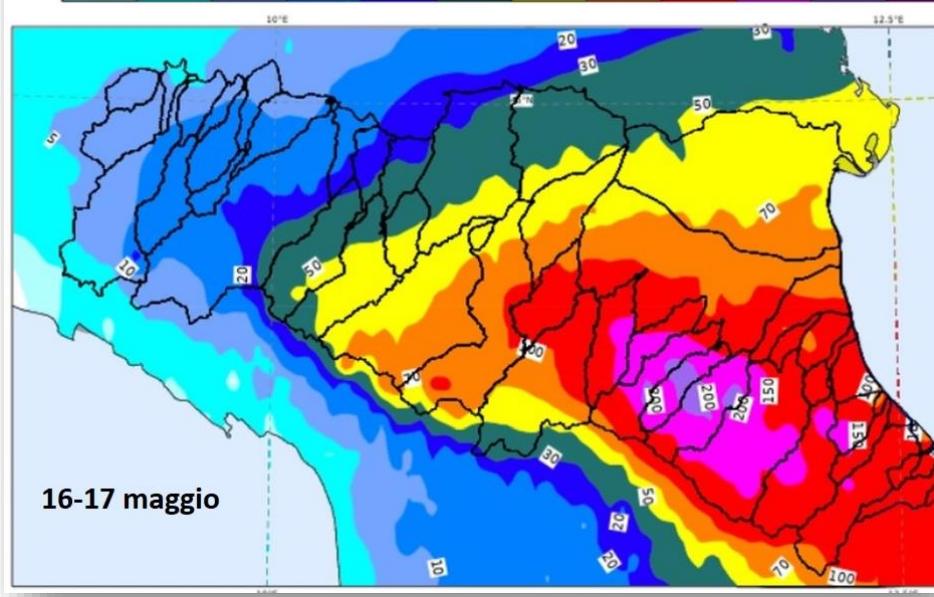
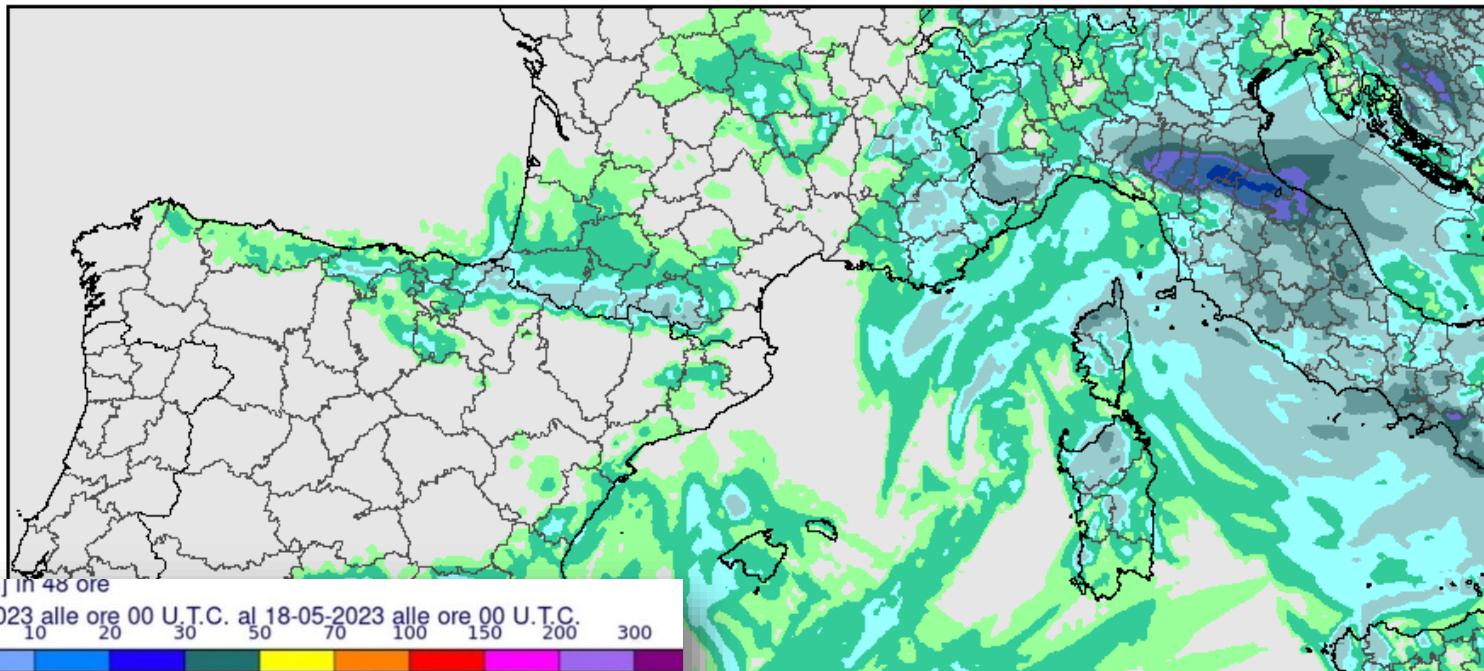
Universitat
de les Illes Balears

EMILIA-ROMAGNA Catastrophic Floods (16-17 May 2023)

TOTAL ACCUM PRECIP (mm)

Forecast: 72:00h / Valid: 00:00z Fri, 19 May 2023

TRAM-HR



ARPAE-SIMC

THANK YOU
for
your attention